OBSERVATIONAL ASTRONOMY

AUTUMN 2022

Lecture 10 short

Vitaly Neustroev

Colour indices (1)

- **Colour indices**: this is the difference between magnitudes at two separate wavelengths:

$$C_{BV} = B - V; \; C_{VR} = V - R, \text{ and so on.}$$

- International colour index (outdated, but can be found in the literature) based upon photographic and photovisual magnitudes:

$$m_p - m_{pv} = C = B - V - 0.11$$

Colour indices (2)

- The B – V colour index is closely related to the spectral type with an almost linear relationship for main sequence stars.
- For most stars, the B and V regions are located on the long wavelength side of the maximum spectral intensity.
- If we assume that the effective wavelengths of the B and V filters are 4400 and 5500 Å, then using the Planck equation:

$$L_\lambda(T) = \frac{2\,h\,c_0^2}{\lambda^5}\left[\exp\left(\frac{h\,c_0}{\lambda\,k_B T}\right) - 1\right]^{-1}$$

we obtain:

$$B - V \approx -2.5 \log\left[3.05\,\frac{\exp(2.617 \times 10^4/T)}{\exp(3.27 \times 10^4/T)}\right]$$

Colour indices (3)

- For $T < 10000$ K this is approximately

$$B - V \approx -2.5 \log\left[3.05 \frac{\exp(2.617 \times 10^4/T)}{\exp(3.27 \times 10^4/T)}\right] = -1.21 + \frac{7090}{T}$$

The magnitude scale is an arbitrary one.
For T = 9600 K (Vega temperature), $B–V = 0.0$,
but we have obtained ~0.5. Using this correction, we get:

$$T = \frac{7090}{(B - V) + 0.74}\ K$$

Colour excess and Interstellar absorption

- More distant stars are affected by interstellar absorption, and since this is strongly inversely dependent upon wavelength.
- The colour excess measure the degree to which the spectrum is reddened:

$$E_{U-B} = (U - B) - (U - B)_0$$

$$E_{B-V} = (B - V) - (B - V)_0$$

where the subscript 0 denotes unreddened quantities – intrinsic colour indices.

- In the optical spectrum, interstellar absorption varies with both wavelength and the distance like this semi-empirical relationship:

$$A_\lambda = 6.5\times10^{-10} / \lambda - 2.0\times10^{-4} \text{ mag pc}^{-1}$$

where λ is in nanometers

Photometry

- Simple UBV photometry for hot stars results in determinations of temperature, Balmer discontinuity, spectral type, and reddening. From the latter we can estimate distance.
- Thus, we have a very high return of information for a small amount of observational effort. This is why the relatively crude methods of wideband photometry is so popular.

Photometry

Effective wavelengths (for an A0 star like Vega), absolute fluxes (corresponding to zero magnitude) and zeropoint magnitudes for the UBVRIJHKL Johnson-Cousins system

Bessel et al.
(1998, A&A, 333, 231)

Band	λc (Å)	f_ν	f_λ	$zp(f_\lambda)$	$zp(f_\nu)$
U	3660	1.790	417.5	0.770	-0.152
B	4380	4.063	632.0	-0.120	-0.602
V	5450	3.636	363.1	0.000	0.000
R	6410	3.064	217.7	0.186	0.555
I	7980	2.416	112.6	0.444	1.271
J	12200	1.589	31.47	0.899	2.655
H	16300	1.021	11.38	1.379	3.760
K	21900	0.64	3.961	1.886	4.906
L	34500	0.285	0.708	2.765	6.775

f_ν (10^{-20} erg $s^{-1} cm^{-2}$ Hz^{-1})
$mag_\lambda = -2.5 \log (f_\lambda) - 21.100 - zp(f_\lambda)$

f_λ (10^{-11} erg $s^{-1} cm^{-2}$ $Å^{-1}$)
$mag_\nu = -2.5 \log (f_\nu) - 48.585 - zp(f_\nu)$

Photometry: Fun with Units (1)

- **Why do we continue to use magnitudes?**
  - Historical reasons: astronomers have built up a vast literature of catalogues and measurements in the magnitude system.
  - The magnitude system is logarithmic, which turns the huge range in brightness ratios into a much smaller range in magnitude differences: the difference between the Sun and the faintest star visible to the naked eye is only 32 magnitudes.
  - Simplicity: Astronomers have figured out how to use magnitudes in some practical ways which turn out to be easier to compute than the corresponding brightness ratios.
- However, in general converting between different magnitude and photometric systems is difficult: conversion factors depend on the spectrum of each object.

Photometry: Fun with Units (2)

- Astronomers who study objects outside the optical wavelengths do not have any historical measurements to incorporate into their work.
- In those regimes, measurements are almost always quoted in "more rational" systems: units which are linear with intensity (rather than logarithmic) and which become larger for brighter objects:

  - erg $s^{-1}cm^{-2}$ $Å^{-1}$
  - erg $s^{-1}cm^{-2}$ Hz^{-1}

  - 1 Jansky [Jy] = 10^{-26} W m^{-2} Hz^{-1} = 10^{-23} erg $s^{-1}cm^{-2}$ Hz^{-1}
    F_ν [Jy]=3.34×10^4 λ^2 F_λ [erg s^{-1} cm^{-2} $Å^{-1}$]
    F_λ [erg s^{-1} cm^{-2} $Å^{-1}$]= 3.00×10^{-5} λ^{-2} F_ν [Jy]

Photometry: Fun with Units (3)

- Fluxes for a V = 0 star of spectral type A0 V at 5450 Å:
  - $f^0_\lambda = 3.63 \times 10^{-9}$ erg $s^{-1} cm^{-2}$ $Å^{-1}$, or
  - $\varphi^0{}_\lambda = f^0_\lambda / h\nu = 996$ photons $s^{-1} cm^{-2}$ $Å^{-1}$

  - Useful:
    - 1 Jy = $1.51 \times 10^3 / \lambda$ photons $s^{-1} cm^{-2}$ $Å^{-1}$
    - $\Delta\lambda / \lambda$ = 0.15 (U), 0.22 (B), 0.16 (V), 0.23 (R), 0.19 (I)

Night Sky Brightnesses

Lunar Age (days)	U	B	V	R	I
0	22.0	22.7	21.8	20.9	19.9
3	21.5	22.4	21.7	20.8	19.9
7	19.9	21.6	21.4	20.6	19.7
10	18.5	20.7	20.7	20.3	19.5
14	17.0	19.5	20.0	19.9	19.2

Signal from the sky background is present in every pixel of the aperture. Because each instrument generally has a different pixel scale, the sky brightness is usually tabulated for a site in units of mag/arcsecond^2.