

# ASTROPHYSICS OF INTERACTING BINARY STARS

**Lecture 13**

Vitaly Neustroev

**360**

# **Non-magnetic Nova-like Variables**

# Nonmagnetic Nova-like Variables

361

- Non-magnetic Nova-like variables (NL) resemble novae between eruptions;
- NLs include all of the “non-eruptive” CVs.
  - ▣ However, many of them may have “low states”
  - ▣ However, some may also exhibit “stunted” outbursts

# Nova-like Variables

362

The NL class is a very heterogeneous group of stars, and the definition of the subclasses within NLs is mostly based on **observational features** of objects.

## □ **Classification:**

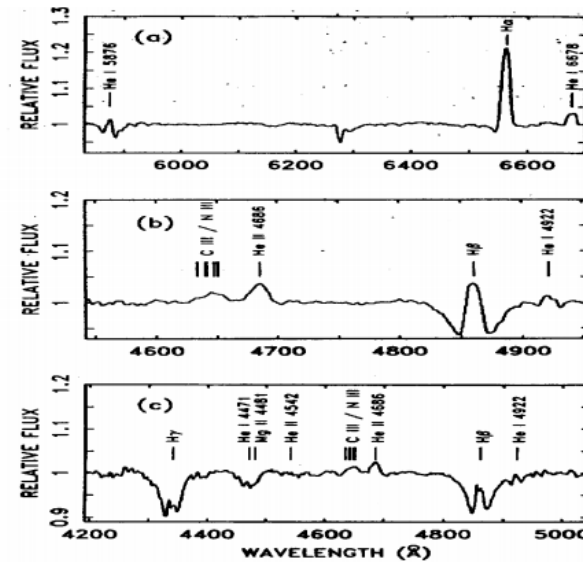
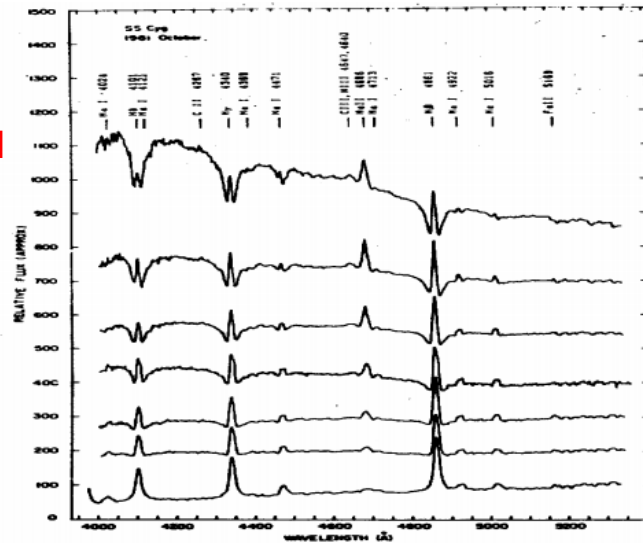
- The UX Ursae Majoris stars (UX UMa) show persistent broad Balmer absorption lines.
- The RW Triangulum stars (RW Tri), per contra, have pure emission-line spectra.
- SW Sextantis stars (SW Sex) show many unusual yet consistent properties (will discuss later).
- VY Sculptoris stars (VY Scl) show states of low luminosity (drops) exceeding 1 mag.

The absence of DN outbursts in NLs is believed to be due to their high mass transfer rates, producing ionised accretion disks in which the disk instability mechanism is suppressed.

# Nova-like Variables

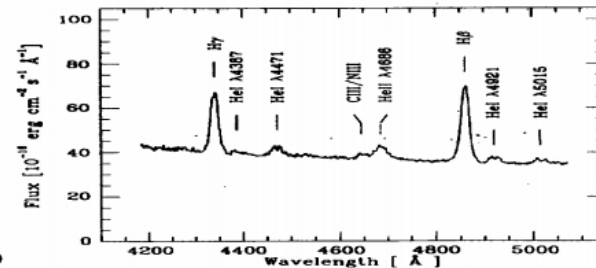
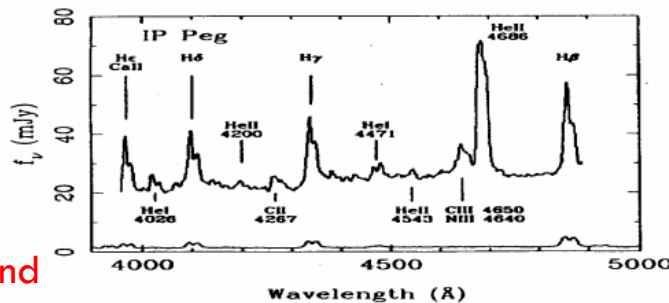
363

The DN  
SS Cyg in  
outburst and  
quiescence



The UX UMa-star  
IX Vel

The DN  
IP Peg in  
outburst and  
quiescence



The SW Sex-star  
WX Ari

# SW Sextantis stars

364

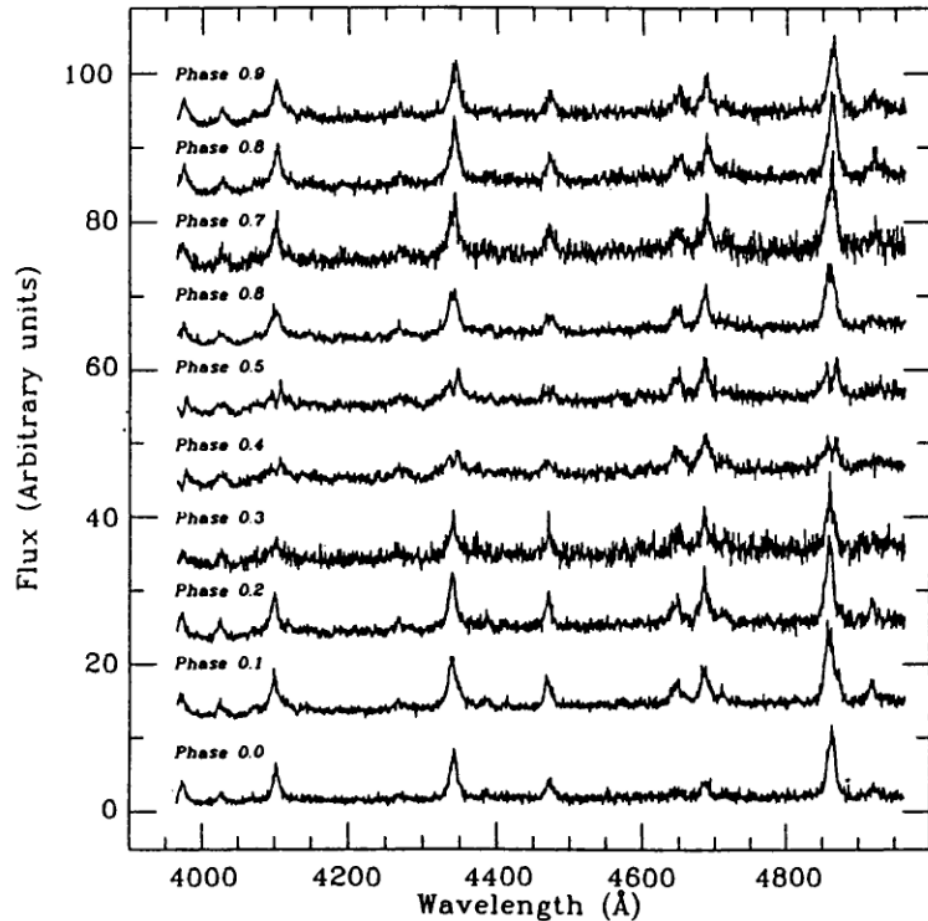
- Relatively large group of NLs, which was initially populated by eclipsing systems only (**high inclination!**);
- Largely occupy the narrow orbital period stripe between 3 and 4.5 hours;
- Single-peaked emission lines despite the high inclination;
- Strong high excitation spectral features (He II, C III/N III);
- Central absorption dips in the emission lines around phase 0.4 – 0.7;
- High-velocity emission S-waves with maximum blueshift near phase  $\sim 0.5$ .

# SW Sextantis stars

365

Time-resolved spectra of  
V1315 Aql.

From  
Dhillon, Marsh & Jones  
(1991).



# SW Sextantis stars

366

- The unusual spectroscopic behaviour of the SW Sex systems has led to their intensive studies.
- Many NLs above the 3 – 4.5 hr period interval have been found to show distinctive SW Sex behaviour;
- Even some LMXBs!
- Even the proto-typical NL UX UMa!



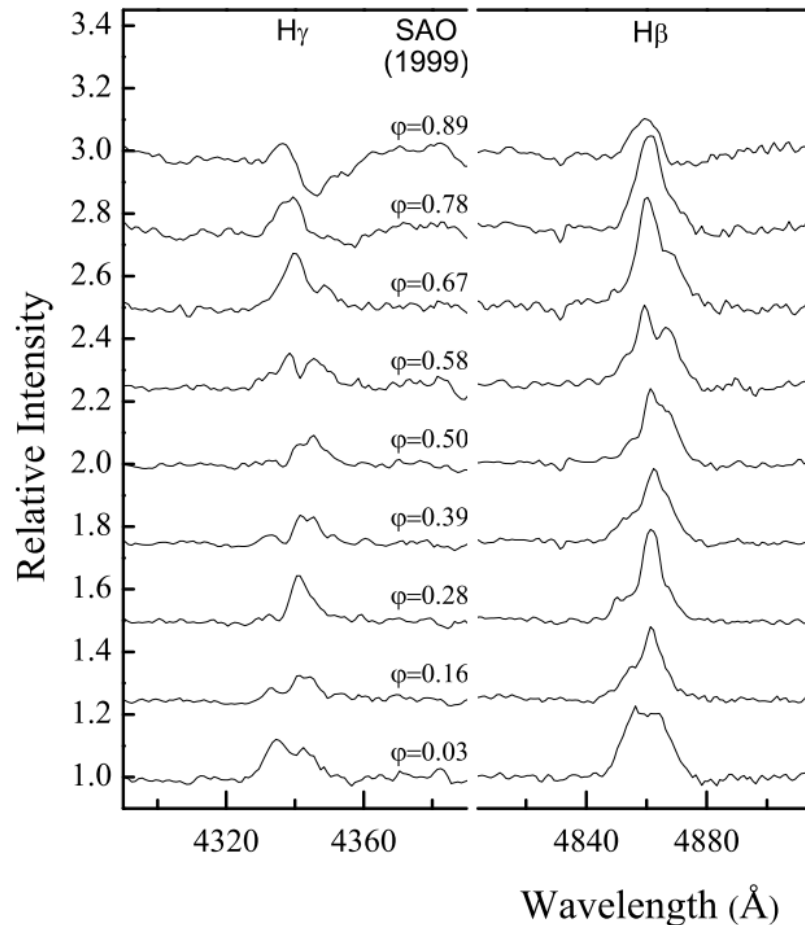
# SW Sextantis stars

367

Even the proto-typical NL UX UMa has now been shown to exhibit SW Sex-like behaviour.

Time-resolved spectra of UX UMa.

From  
Neustroev et al. (2011).



# Nova-like Variables

368

## □ Classification:

- The UX Ursae Majoris stars (UX UMa) show persistent broad Balmer absorption lines.
- The RW Triangulum stars (RW Tri), per contra, have pure emission-line spectra.
- SW Sextantis stars (SW Sex) show many unusual yet consistent properties (will discuss later).
- VY Sculptoris stars (VY Scl) show states of low luminosity (drops) exceeding 1 mag.

**We now suspect that all NLs could be classified as SW Sex stars if one looks long and hard enough.**

369

# Magnetically-Controlled Accretion

Polars

Intermediate Polars

# Magnetically-Controlled Accretion

370

- In some CVs we observe interesting features:
  - ▣ Strongly polarized emission (up to 60 % circular polarisation in the optical);
  - ▣ Strong X-ray emission;
  - ▣ Unexpectedly long soft X-Ray component;
  - ▣ Highly variable light curves in optical and X-Ray;
  - ▣ In some objects: short-period coherent variability.

**⇒ Strong Influence from a magnetic field on the binary system**

# Magnetically-Controlled Accretion

371

- Magnetic Field of the WD in First Approximation:
  - ▣ Both stars have a magnetic field;
  - ▣ The magnetic flux is roughly conserved during star evolution:  $B \cdot R^2 \approx \text{const}$
- ⇒ **High field strengths up to 20MG near the WD;**
- ▣ Magnetic field is usually approximated as a Dipole.

# Magnetically-Controlled Accretion

372

- Important parameter:

The magnetospheric radius,  $R_M$  - the distance from the WD where the magnetic pressure is equal to the ram pressure:

$$\frac{B^2}{8\pi} = \rho(r)v_{in}^2(r)$$

- For polars,  $B_{wd} \sim 10^7$  G,  $R_M \sim 10^{11}$  cm  $\sim a$

**NO DISK!**

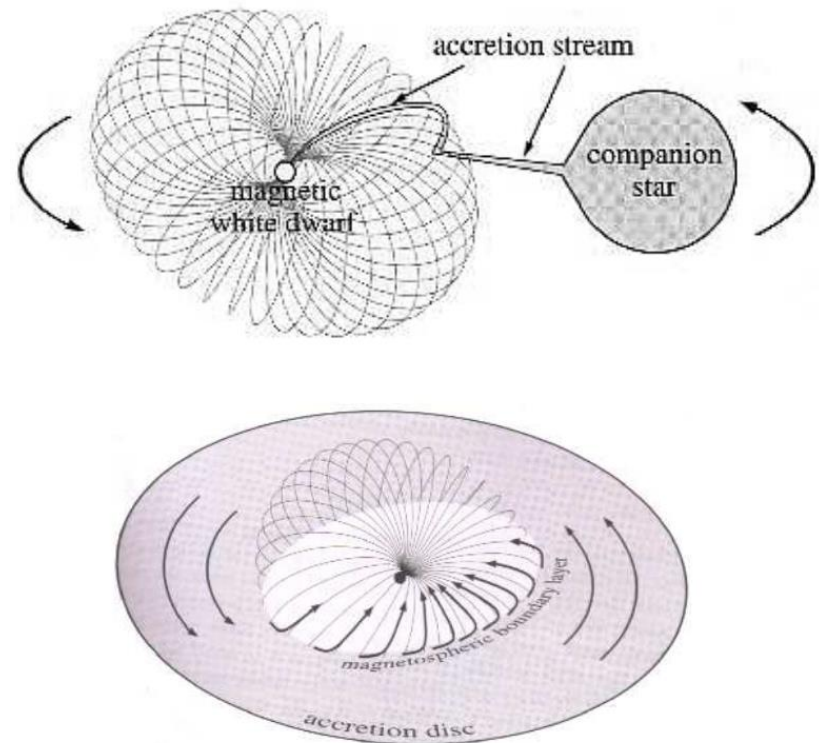
- For intermediate polars,  $B_{wd} \sim 10^6$  G,  $R_M \sim 10^{10}$  cm

**TRUNCATED DISK**

# Magnetically-Controlled Accretion

373

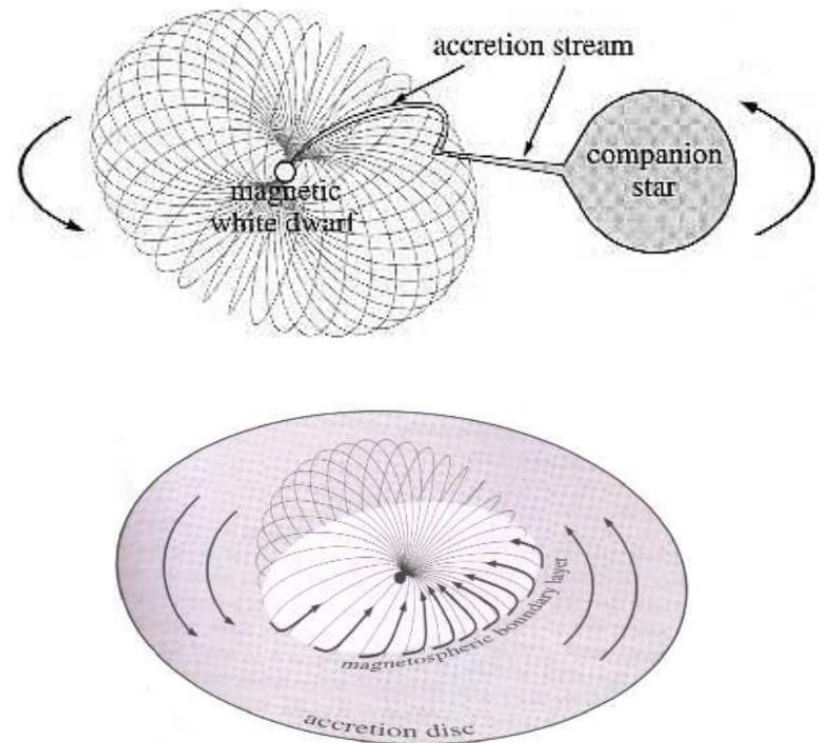
- Pressure balance defines the inner edge of the accretion disk:
  - ▣ For strong magnetic fields of the WD no disk is formed, instead the accretion stream follows the field lines directly;
  - ▣ For weaker magnetic fields a truncated accretion disk will form.
- These two scenarios are called an accretion column and an accretion curtain, respectively.



# Magnetically-Controlled Accretion

374

- The corotation radius is the radius at which the disk corotates with the magnetic field. This is usually near the inner edge of the disk, which is the magnetospheric radius.





# Magnetically-Controlled Accretion

375

- Spin Periods and Angular Momentum:
    - ▣ System has an orbital period  $P_{\text{orb}}$ ;
    - ▣ the WD has a spin period  $P_{\text{spin}}$ ;
    - ▣ Therefore modulations should be observed;
    - ▣ Accretion stream transfers angular momentum to WD
- ⇒ Spin-up ?**
- ▣ Consider interaction of magnetic moments of the two stars!
  - ▣ Magnetic moments can **balance** transfer of angular momentum, if interaction is strong enough

# Polars

376

## □ **Polars** or **AM Her** Stars:

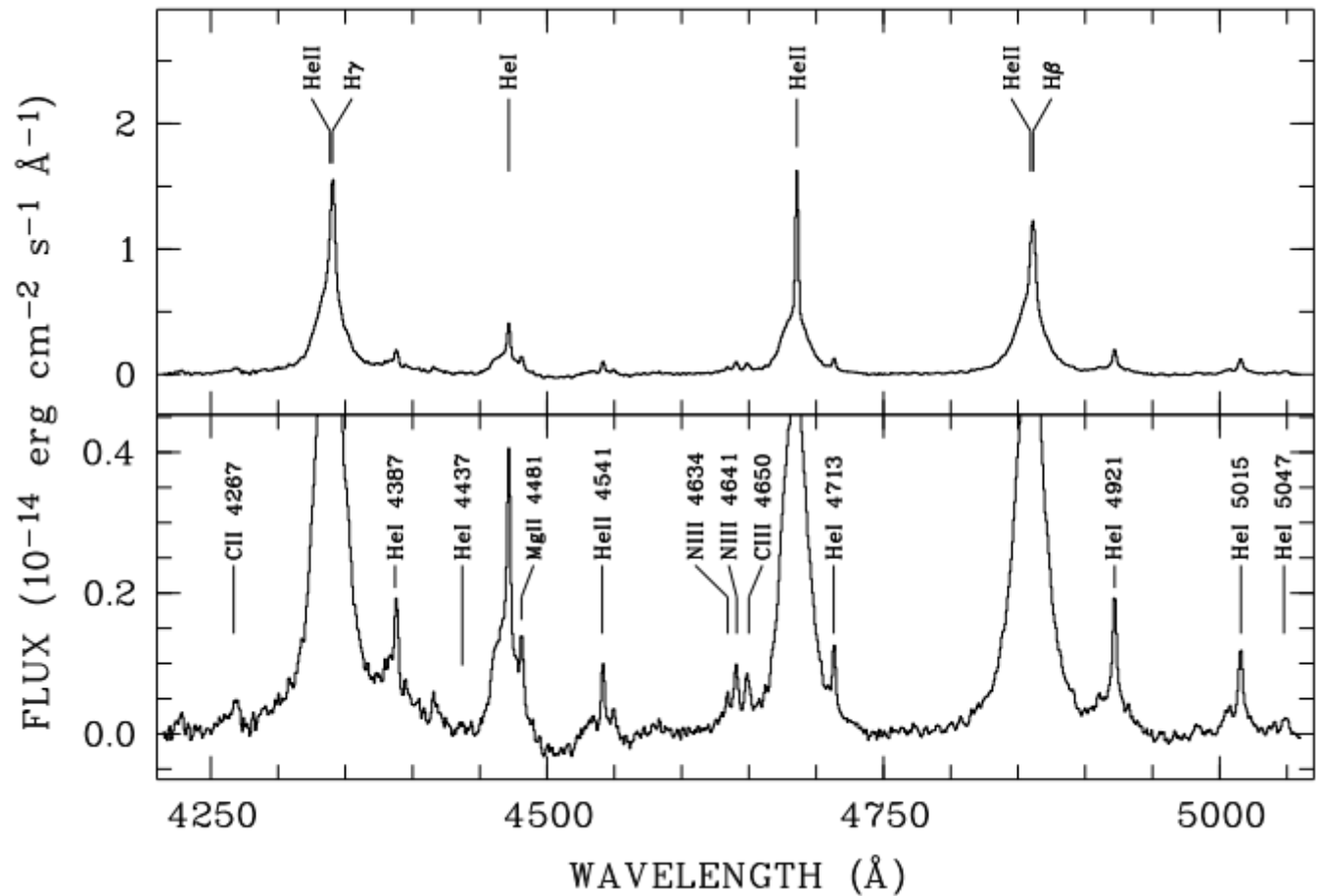
Systems with Strong Magnetic Field and Strong Magnetic Interaction:

- Synchronise orbital period and spin period of the WD, due to magnetic interaction;
- Don't have accretion disks;
- Can be identified through strong polarisation in optical wavelength.

# Polars

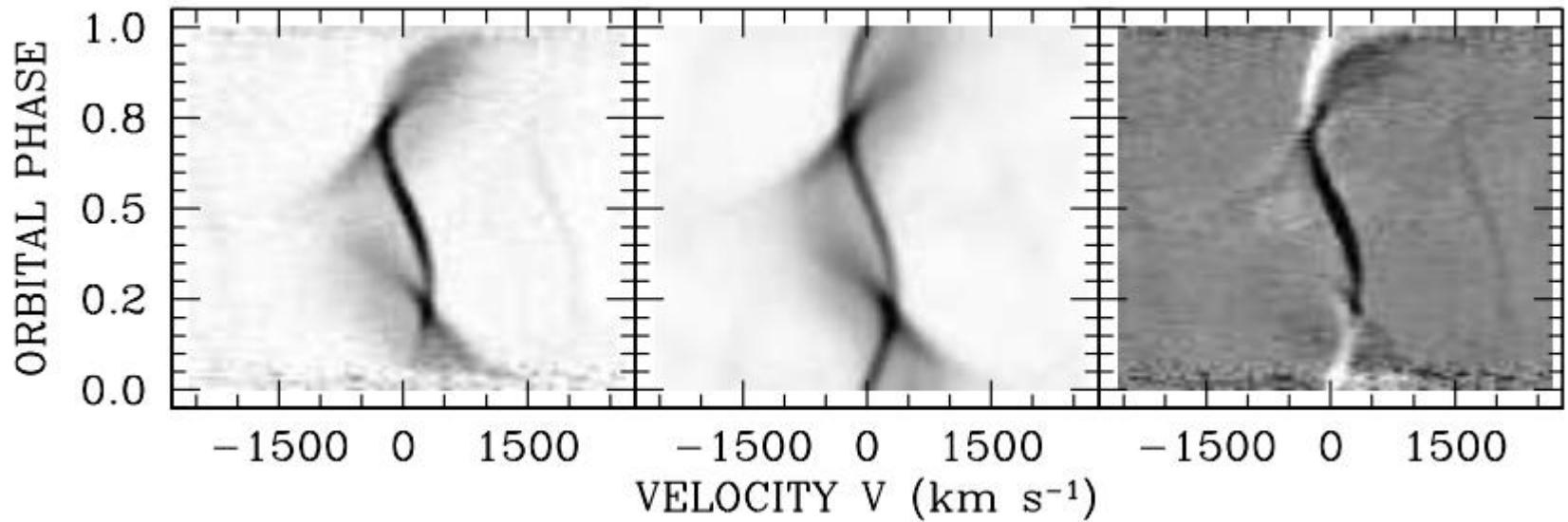
377

Mean-orbital  
high-resolution  
spectrum of  
the polar  
HU Aqr



# Polars

378

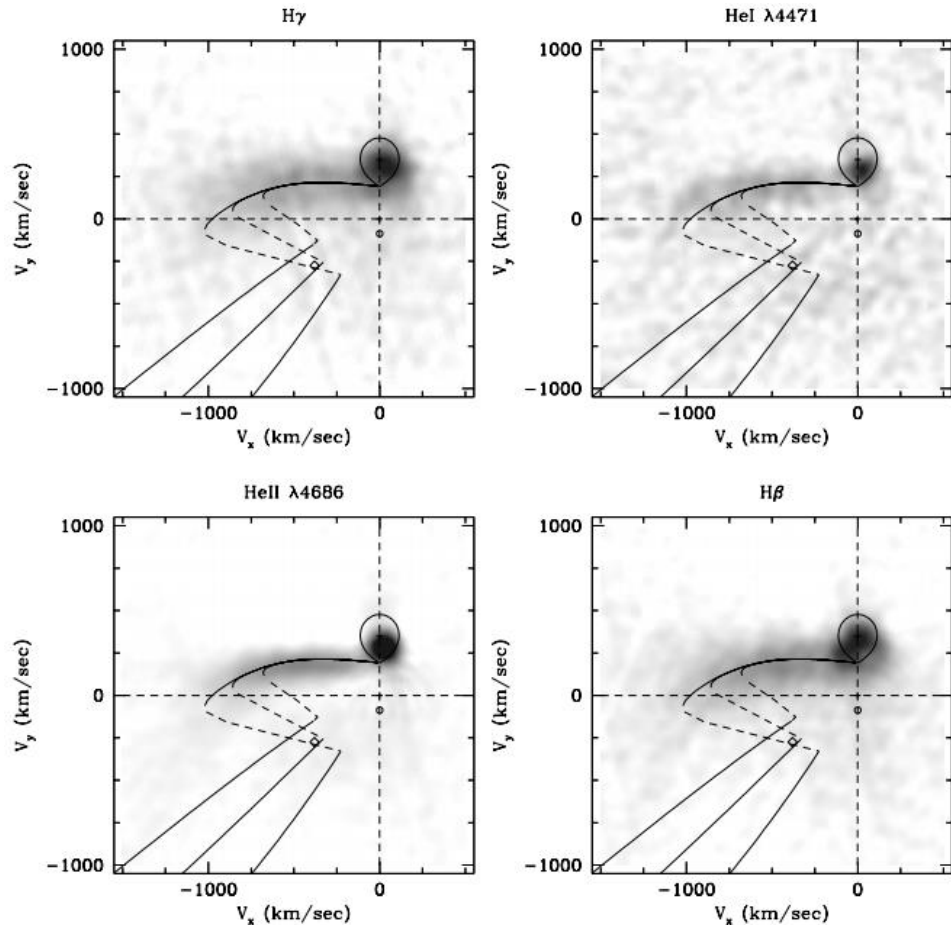


Trailed spectrogram of the He II emission line of the polar HU Aqr

# Polars

379

Doppler maps of the  
four main emission lines  
of the polar HU Aqr



Interacting Binary Stars

# Intermediate Polars

380

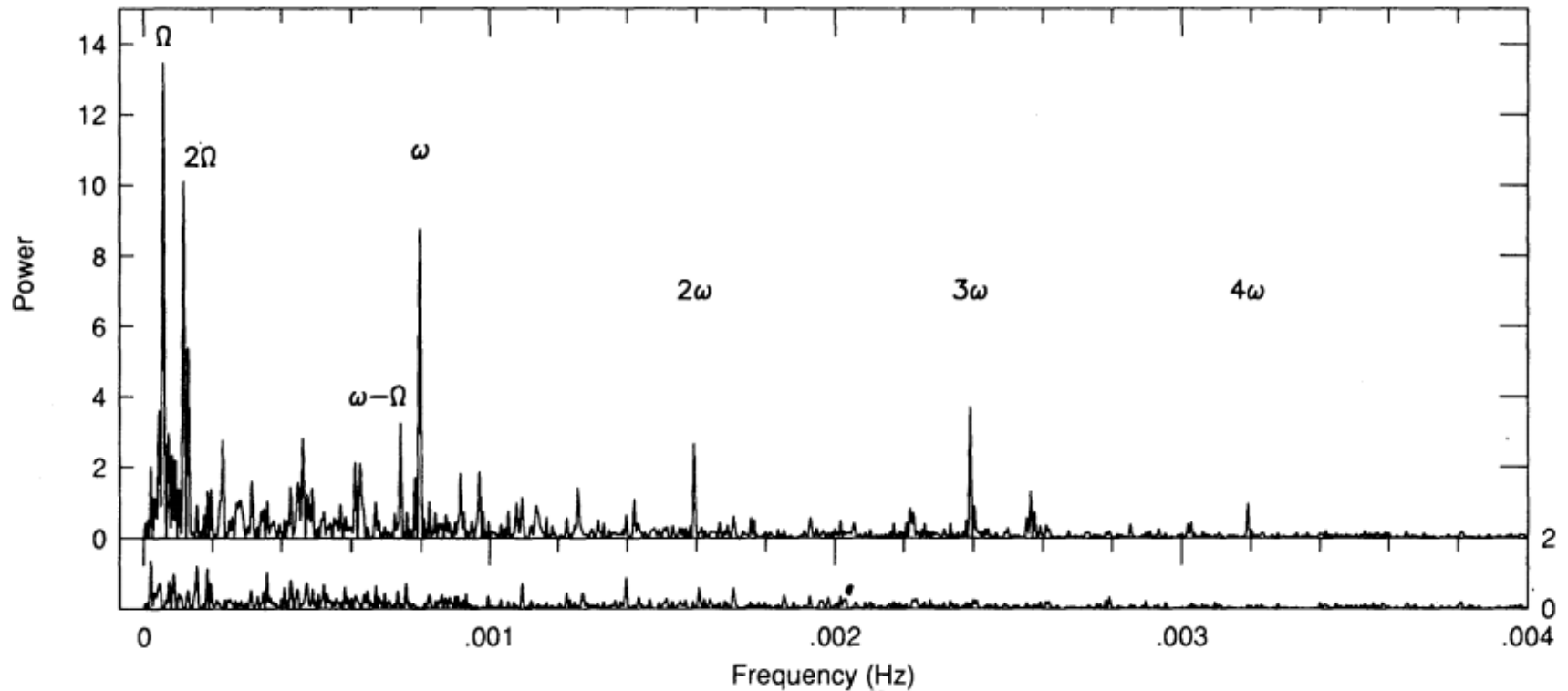
- **Intermediate Polars or DQ Her Stars:**  
Systems with Weaker Magnetic Field:
  - ▣ Low Interaction between magnetic moments;
  - ▣ Spin Up, due to transfer of angular momentum;
  - ▣ No synchronised state of the rotation periods, but rotation at high velocities;
  - ▣ A truncated accretion disk, as magnetic pressure can't control the plasma far enough.

**Not always the case!**

**Video**

# Intermediate Polars

381



The power spectrum of the X-ray light curve of FO Aqr: **multiple periodicities**

382

# AM CVn Binaries



# Close Binary Systems

383

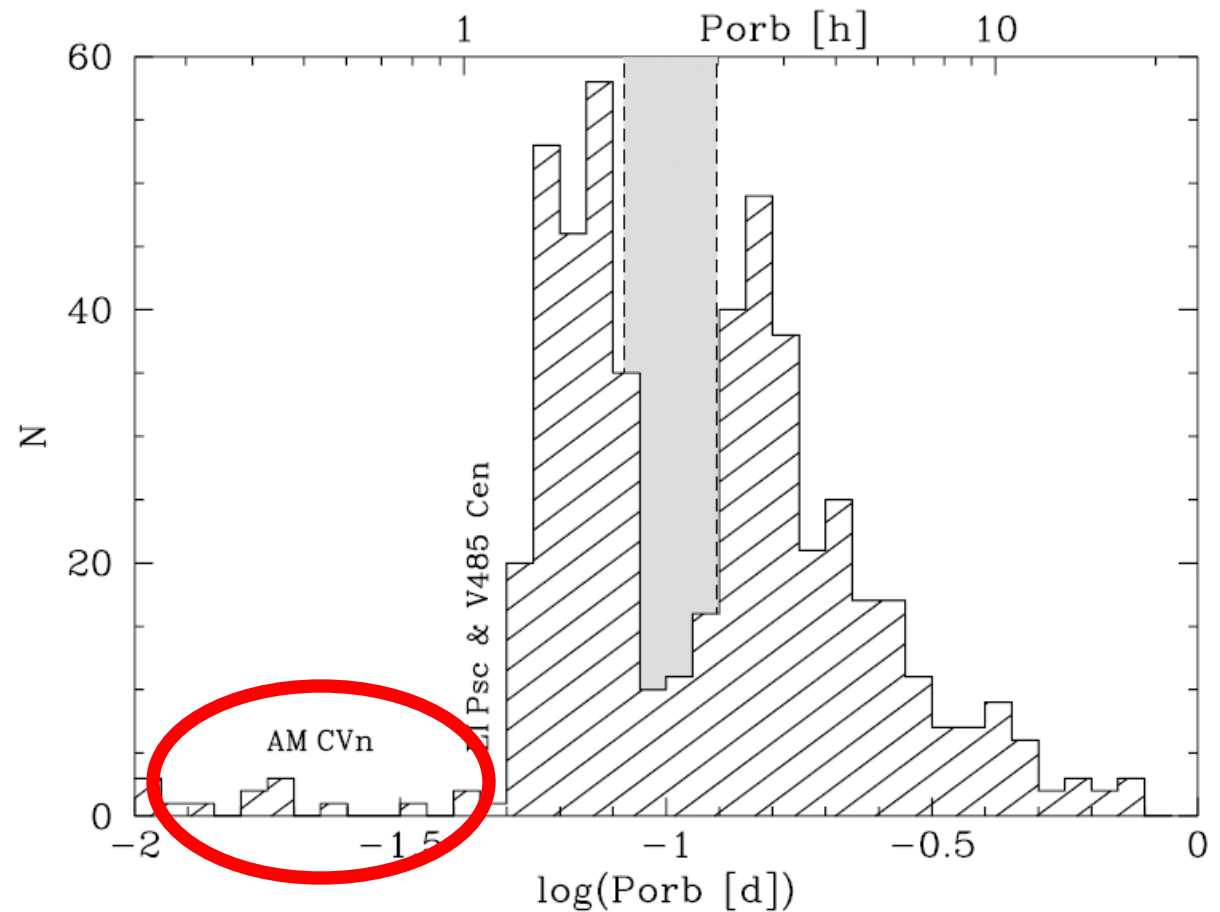
secondary primary	main-sequence star <sup>*)</sup>	evolved star <sup>**)</sup>	white dwarf	neutron star or black hole
main-sequence star <sup>*)</sup>	[binary T Tauri stars] [RS CVn stars] Algols (AD) (TAD) {W UMa stars = contact systems}	symbiotic stars Type I as e.g. CI Cyg, Z And, AR Pav (AD) Algols (AD), (TAD)	<sup>*)</sup> main-sequence star or slightly evolved <sup>**)</sup> evolved star, but not yet a compact star [ ] detached systems (AD) evidence for an accretion disk (TAD) evidence for a transient accretion disk	
evolved star <sup>**)</sup>	[Wolf-Rayet binaries] [binary planetary nebulae ]			
white dwarf	[pre-cataclysmic binaries] non-magnetic CVs: UX UMa stars (AD) dwarf novae (AD) DQ Her stars (AD) AM Her stars	long period CVs as GK Per (AD) recurrent nova (AD) symbiotic stars (AD) symbiotic novae (AD)	[double white dwarfs] AM CVn stars (AD)	
neutron star or black hole	massive X-ray binaries (AD) (wind accretion) low mass X-ray binaries (AD) HZ Her/Her X-1 (AD) SS 433 (AD)	long period low mass X-ray binaries (AD)	[binary pulsars] 4U1820-30 (AD)	[binary pulsars]

Comments: in semi-detached systems the mass gaining star is listed as the primary  
in detached systems the more evolved star is listed as the primary

# CVs: Distribution of Orbital Periods

384

The orbital period distribution of 531 CVs from Ritter & Kolb (2003,V7.3).



# The AM Canum Venaticorum binaries

385

- Key properties:
  - ▣ No hydrogen
  - ▣ Very short periods (5 – 10 to 65 minutes)
  - ▣ Spectra characteristic of accretion disks
  - ▣ Weak X-ray emission
  
- AM CVn binaries are a class of ultracompact systems in which the donor stars are hydrogen deficient. The accretors are white dwarfs.

# AM CVn stars

386

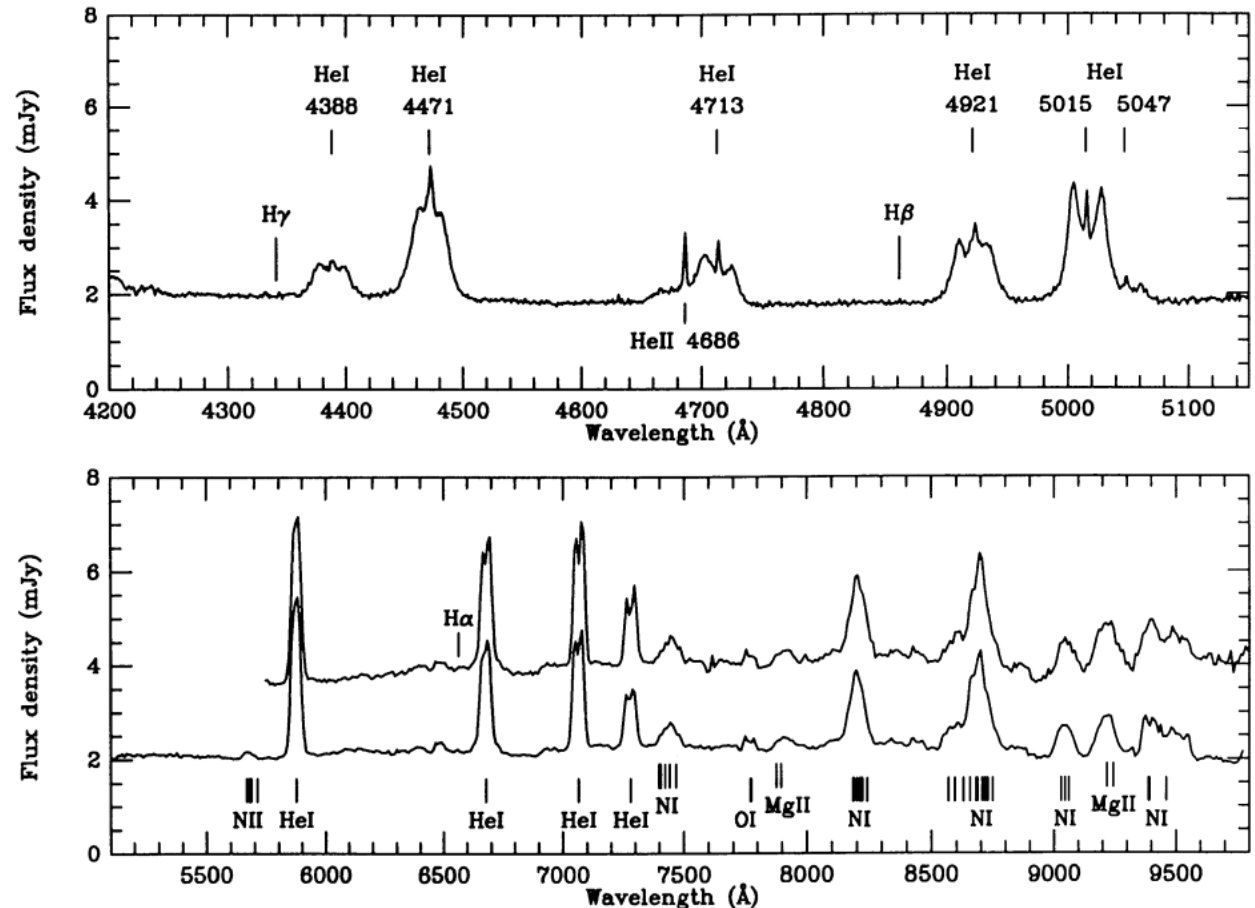
- To fit within their Roche lobes, the donor stars must be dense ( $\bar{\rho}_2 = 100 - 4000 \text{ g cm}^{-3}$ ), suggesting they may be degenerate too:  
“double degenerate” (Faulkner et al 1972).
- Currently 56 known AM CVn systems.  
(Ramsay et al., 2018, A&A, 620, A141)

# Spectra of AM CVn's

387

The most obvious observational signature is their optical spectrum - lack of hydrogen lines.

GP Com,  $P=46$  min  
(Marsh et al. 1991)

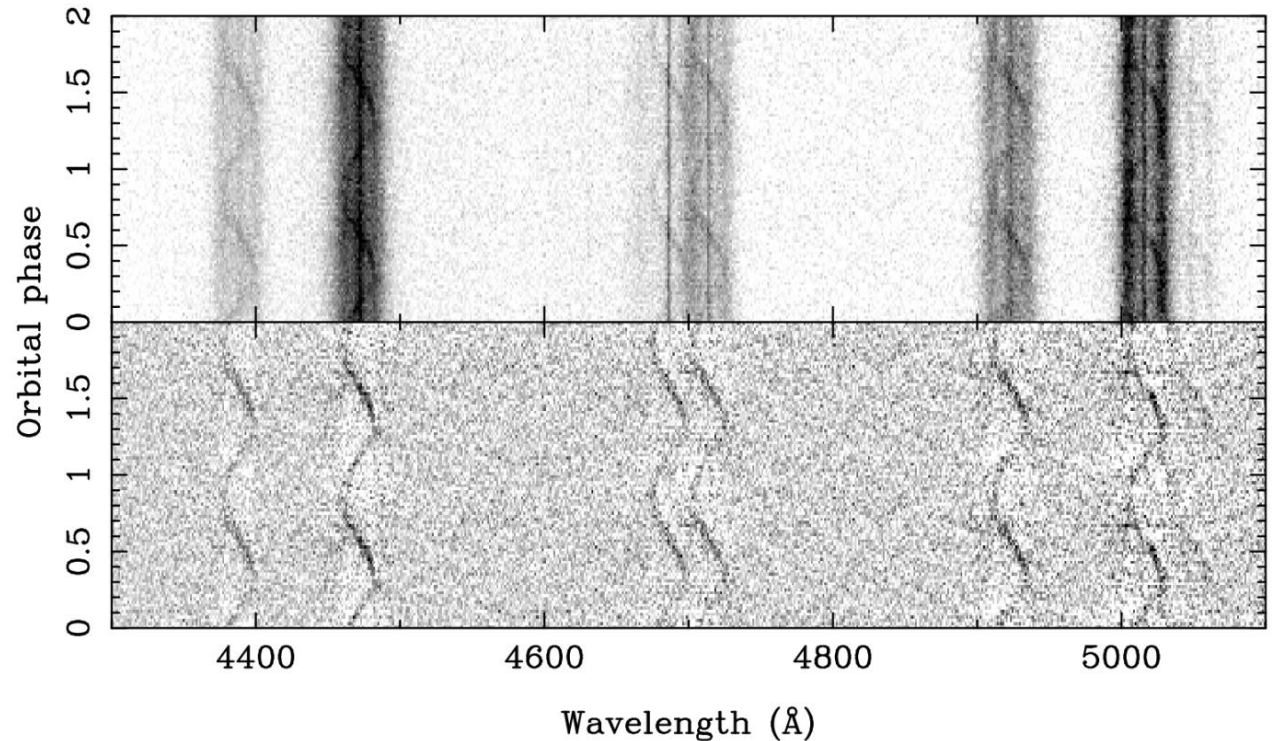


# Spectra of AM CVn's

388

The most obvious observational signature is their optical spectrum - lack of hydrogen lines.

GP Com,  $P=46$  min  
(Marsh et al. 1991)



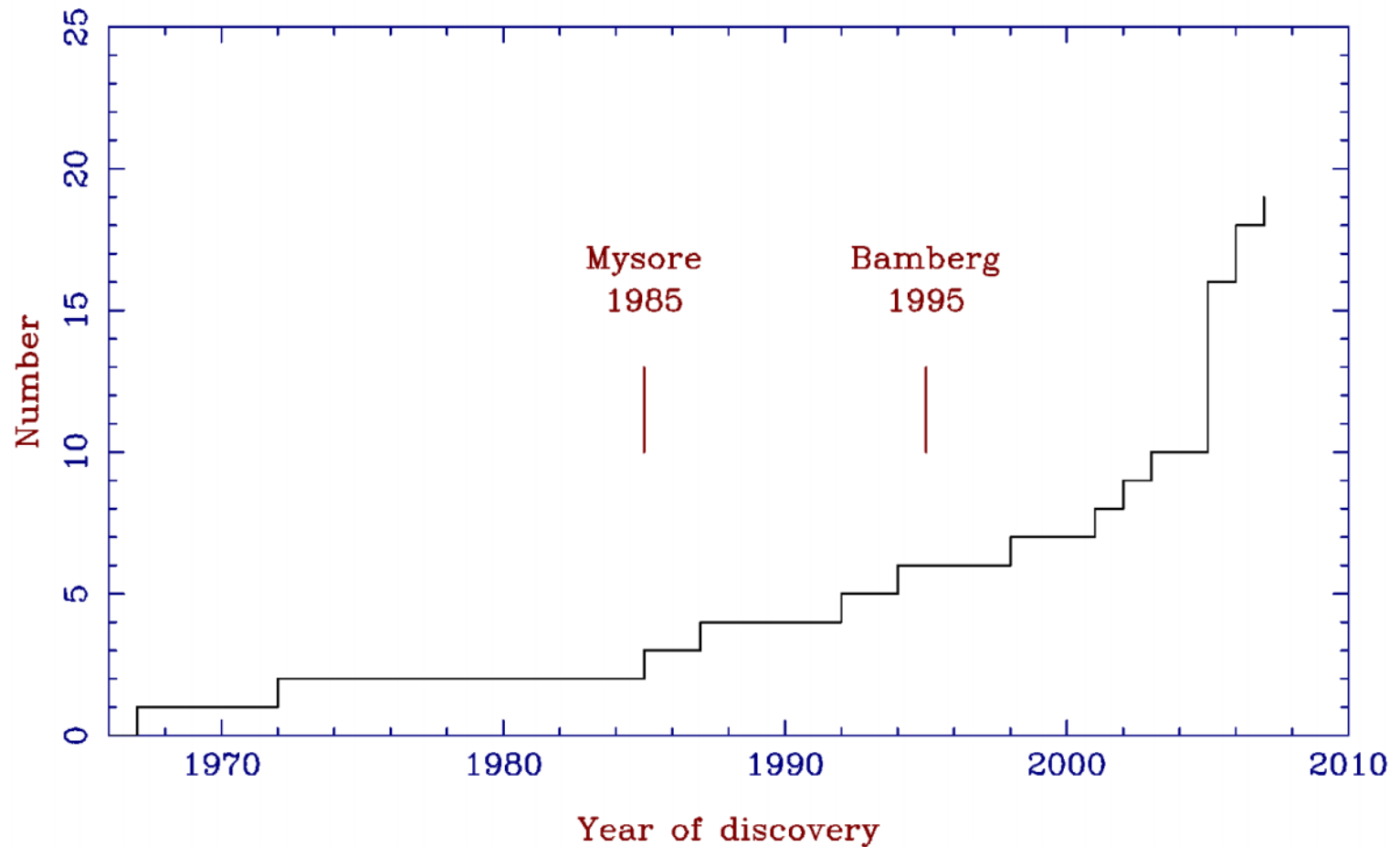
# AM CVn stars

389

- Total number in Galaxy:  $3 \times 10^5 - 3 \times 10^6$  (Roelofs et al 2007)
- Accreting white dwarfs:  $M_1 \sim 0.6M_\odot$
- Mass donors:  $M_2 = 0.015 - 0.15M_\odot$
- Orbital separations:  $a = 0.1 - 0.4 R_\odot$
- Disk size:  $R_d \sim 0.35a$
- Mass transfer rates:  $\dot{M} = 10^{-12} - 10^{-8} M_\odot / \text{yr}$
- Absolute magnitudes:  $M_V = 5 - 13$

# AM CVn stars: Discovery history

390

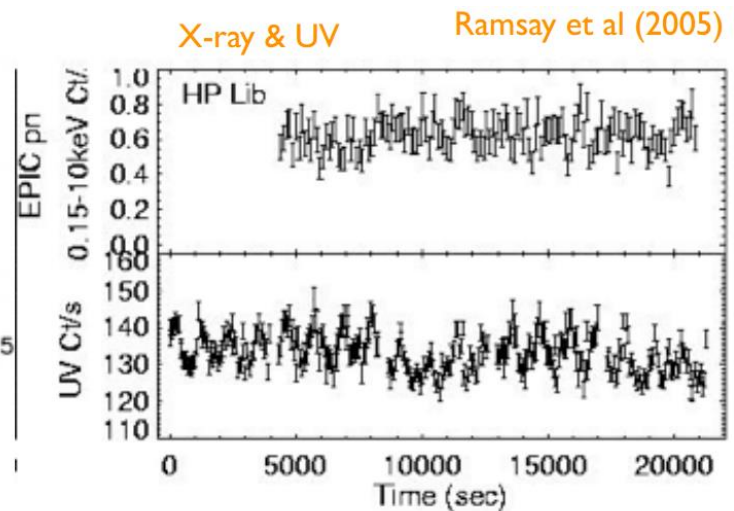
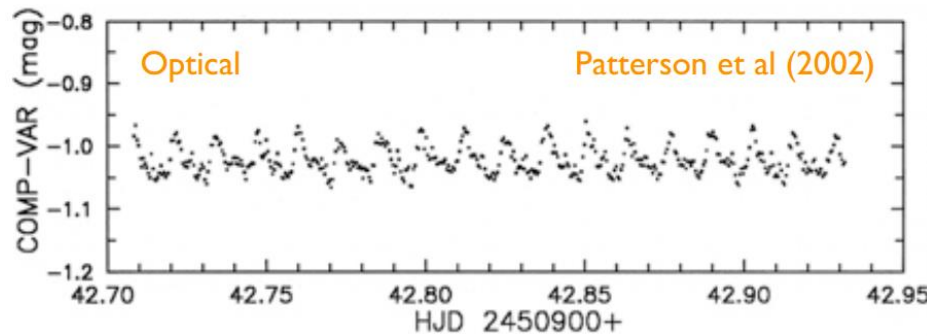




# Light curves of AM CVn's

391

- Can be split into systems in low state, high state and those which undergo outbursts. Systems in outburst and in a high state show characteristic modulations in their optical light curve.



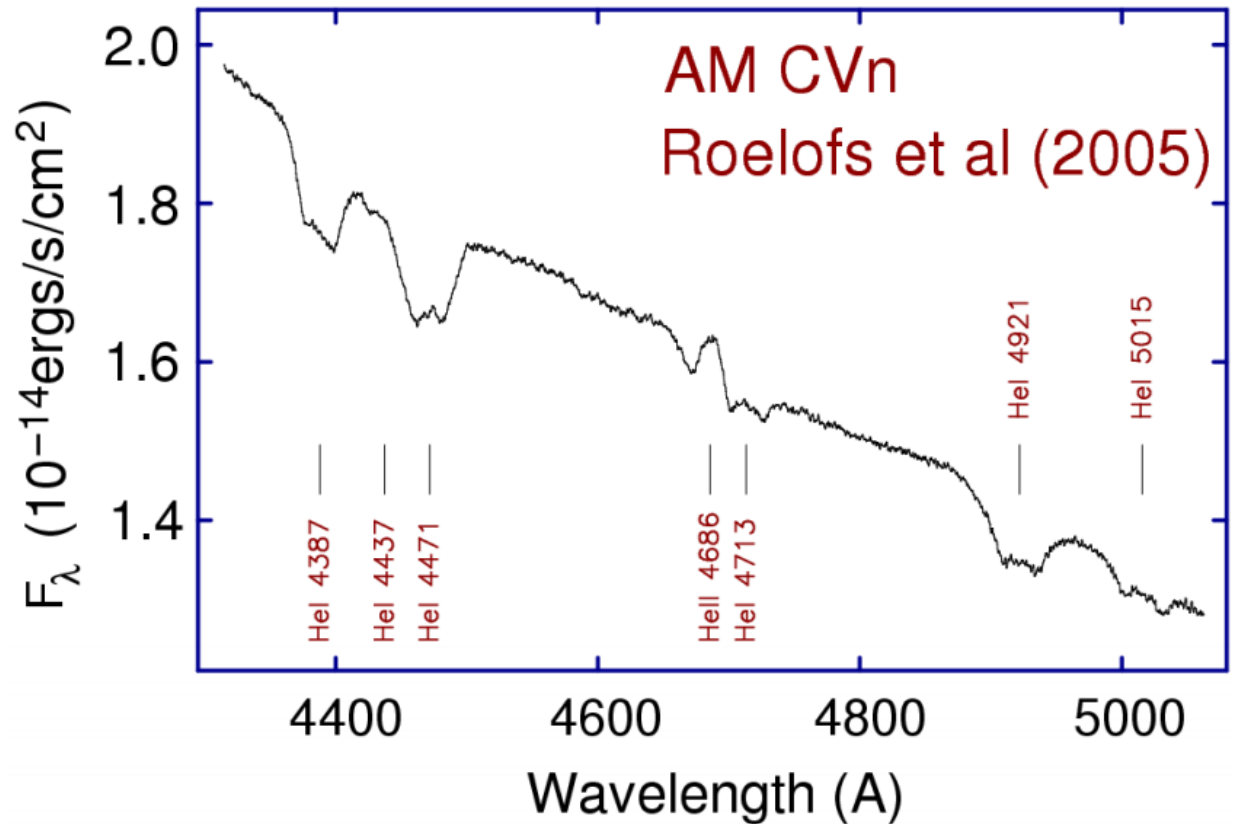
HP Lib ( $P_{orb}=18.4\text{min}$ ) Optical and UV light curves show modulation due to precession period of the accretion disc.

# Three groups of AM CVn's

392

AM CVn stars split into three groups:

1) High  $\dot{M}$ , permanently bright, dominated by the accretion disk,  $P < 20$  mins

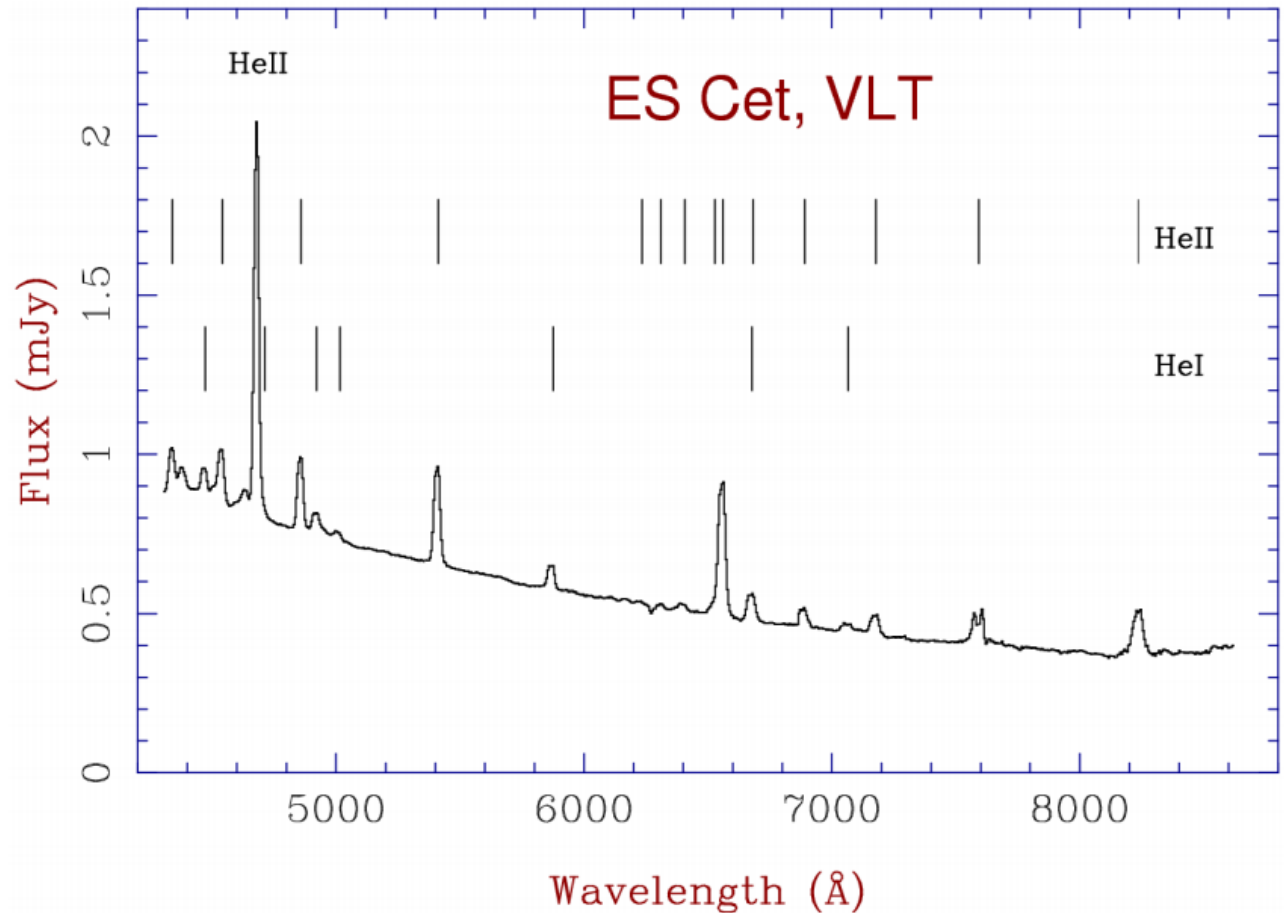


# Three groups of AM CVn's

393

AM CVn stars split into three groups:

1) High  $\dot{M}$ , permanently bright, dominated by the accretion disk,  $P < 20$  mins

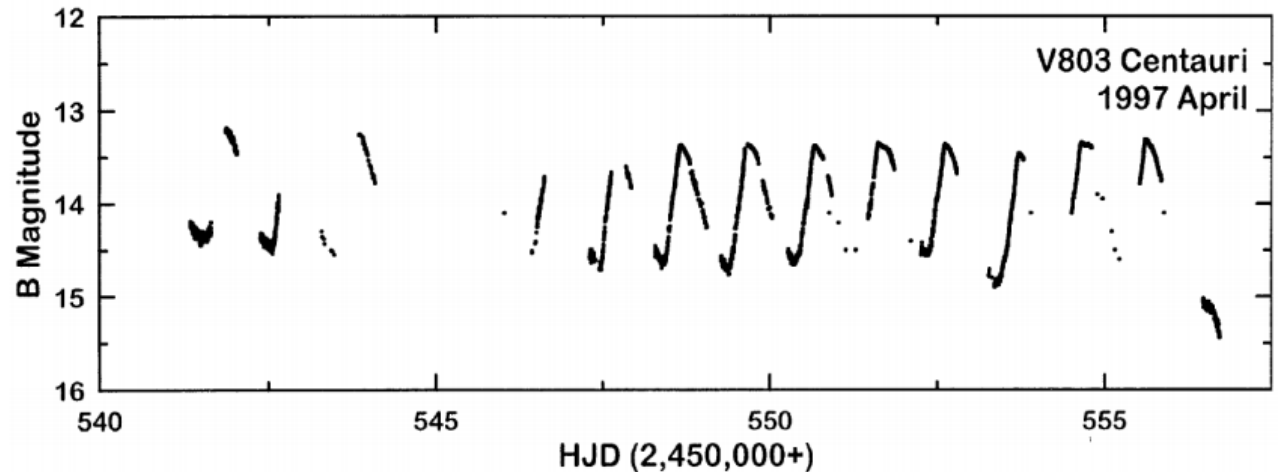


# Three groups of AM CVn's

394

AM CVn stars split  
into three groups:

2) Medium  $\dot{M}$ ,  
“dwarf novae”,  
 $20 < P < 40$  mins



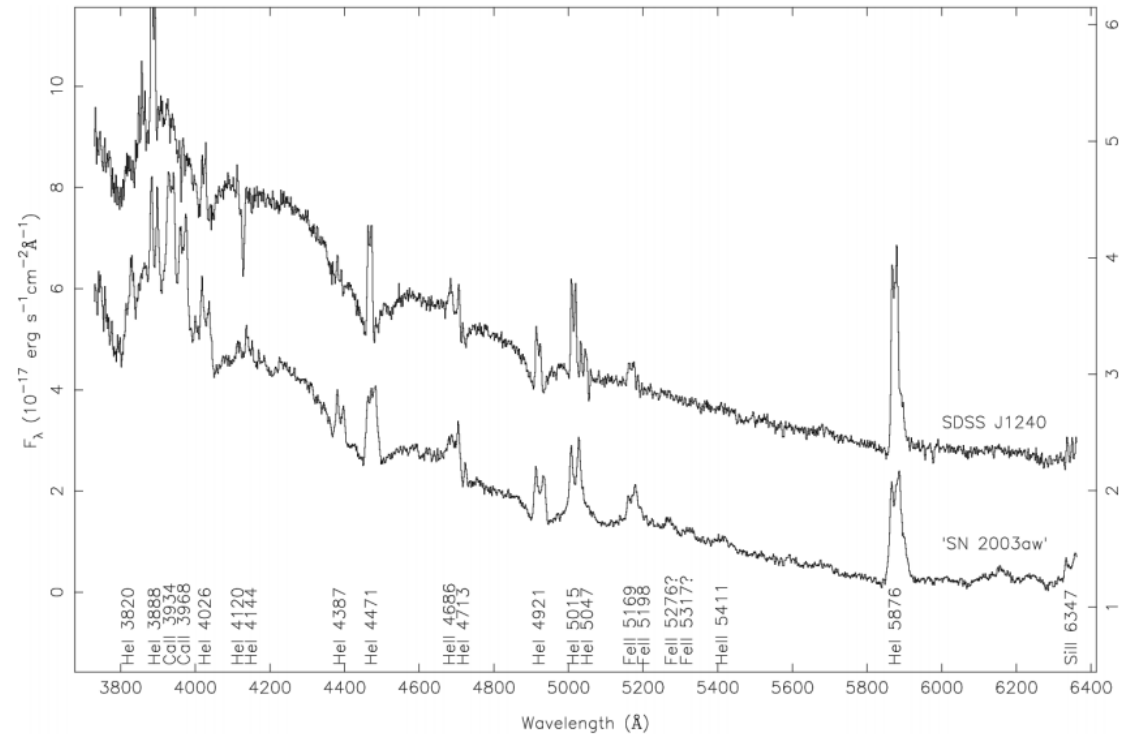
V803 Cen, Patterson et al. (2002)

# Three groups of AM CVn's

395

AM CVn stars split into three groups:

3) Low  $\dot{M}$ ,  
permanently faint.  
Continuum from the  
accreting white  
dwarf, emission  
lines from the disk,  
 $P > 40$  mins



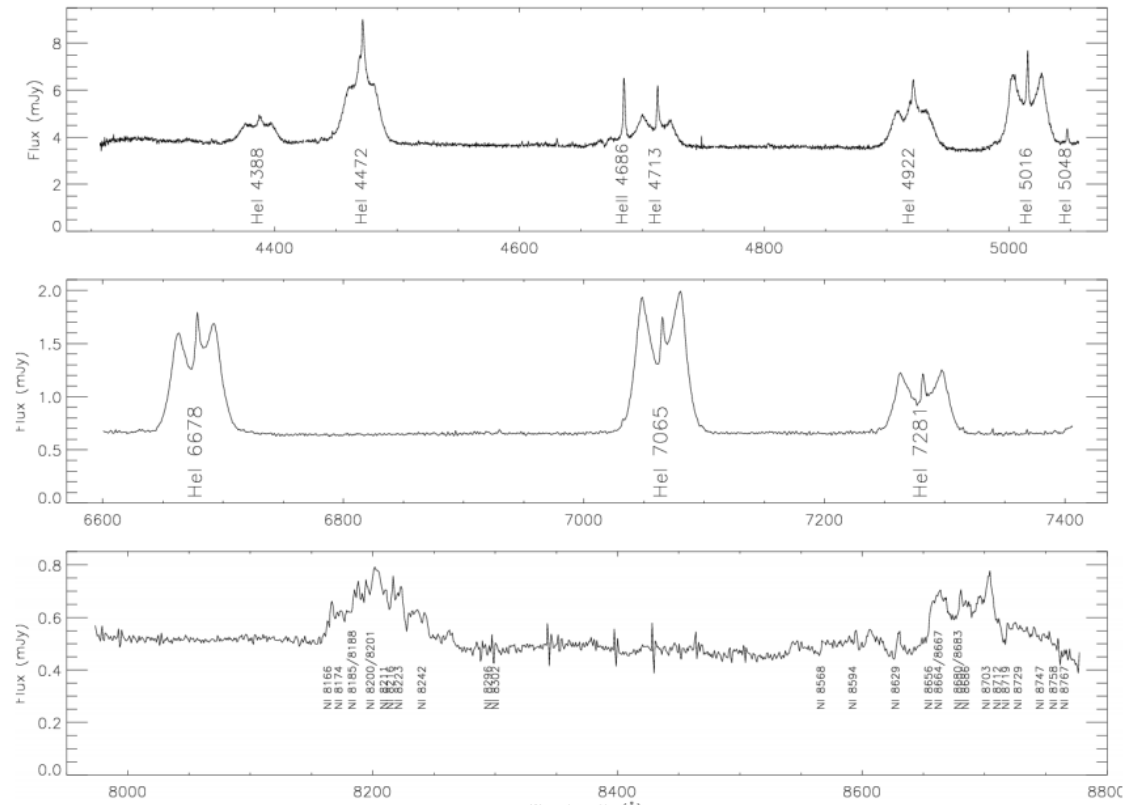
SN 2003aw, SDSS1240, Roelofs et al  
(2005)

# Three groups of AM CVn's

396

AM CVn stars split into three groups:

3) Low  $\dot{M}$ ,  
permanently faint.  
Continuum from the  
accreting white  
dwarf, emission  
lines from the disk,  
 $P > 40$  mins



GP Com, Morales-Rueda et al (2003)

# Orbital period/accretion rate relation

397

If

- (a) the donors in AM CVn stars are degenerate,
- (b) mass transfer is driven by gravitational radiation, and
- (c)  $M_2 \ll M_1$ :

□ Can eliminate  $a$ ,  $R_2$  and  $M_2$  to show:

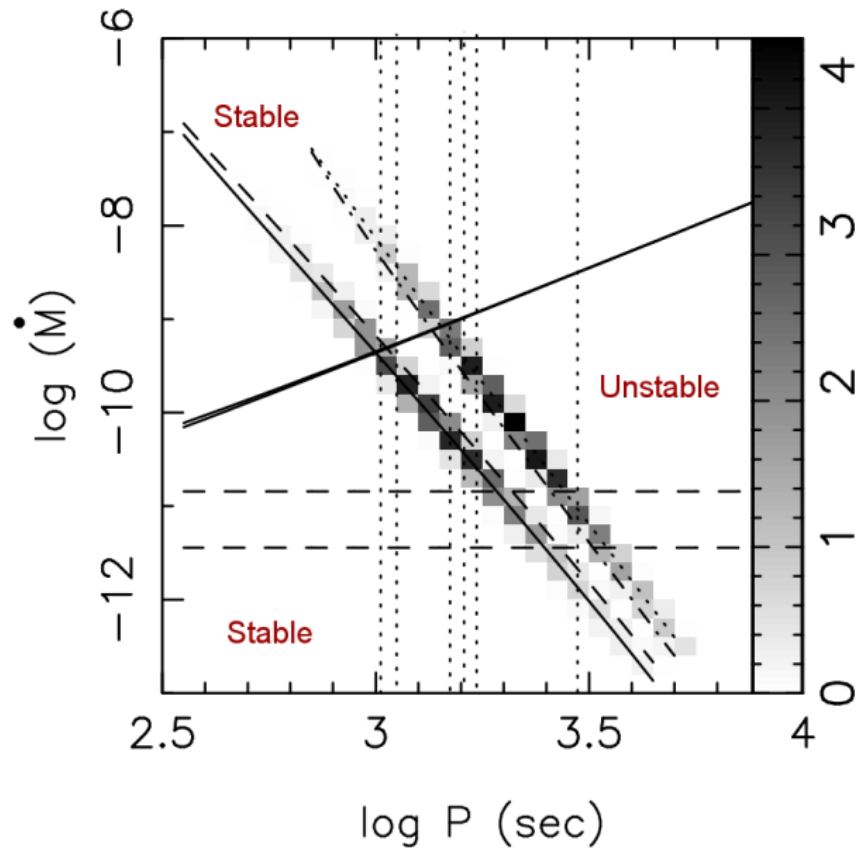
$$\dot{M}_{accr} \propto P^{-14/3}$$

□  **$\Rightarrow$  AM CVn stars vary much more strongly with orbital period than their hydrogen-rich counterparts.**

# The evolution of AM CVn stars – I.

398

The steep drop of  $\dot{M}$  with period combined with a thermal instability caused by the ionisation of helium (Tsugawa & Osaki 1997) can explain the 3 types of systems.



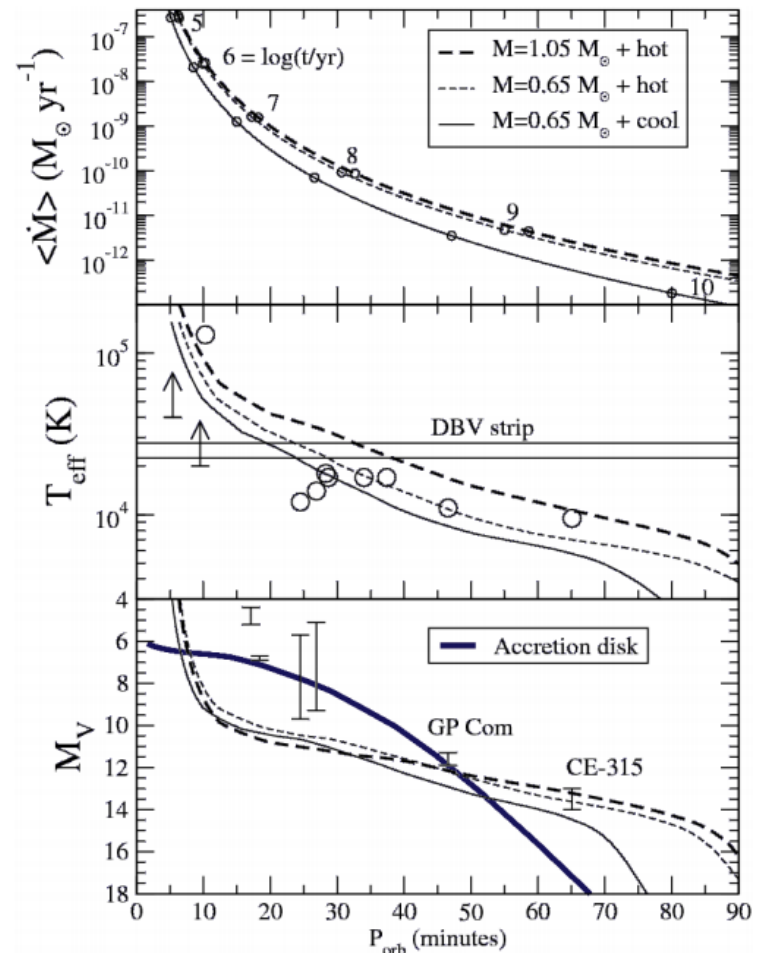
Nelemans et al (2001)



# The evolution of AM CVn stars – II.

399

- The accreting white dwarf's temperature is a combination of normal evolutionary cooling and compressional heating (Bildsten et al 2006).
- It may dominate over the accretion luminosity at both short ( $< 10$  min) and long ( $> 40$  min) orbital periods.



# The first eclipsing AM CVn star

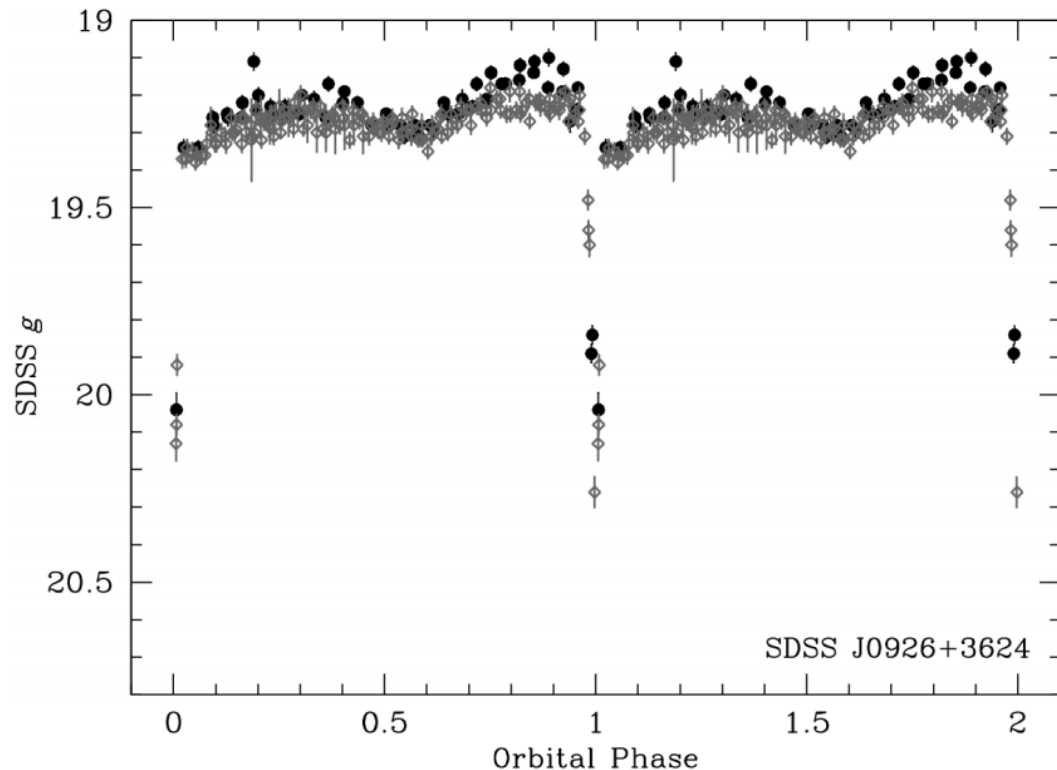
400

**SDSS0926+3624**

$P = 28$  minutes,  
the only eclipsing  
AM CVn known

$g' = 19.3$  with  
eclipses that last 1  
minute.

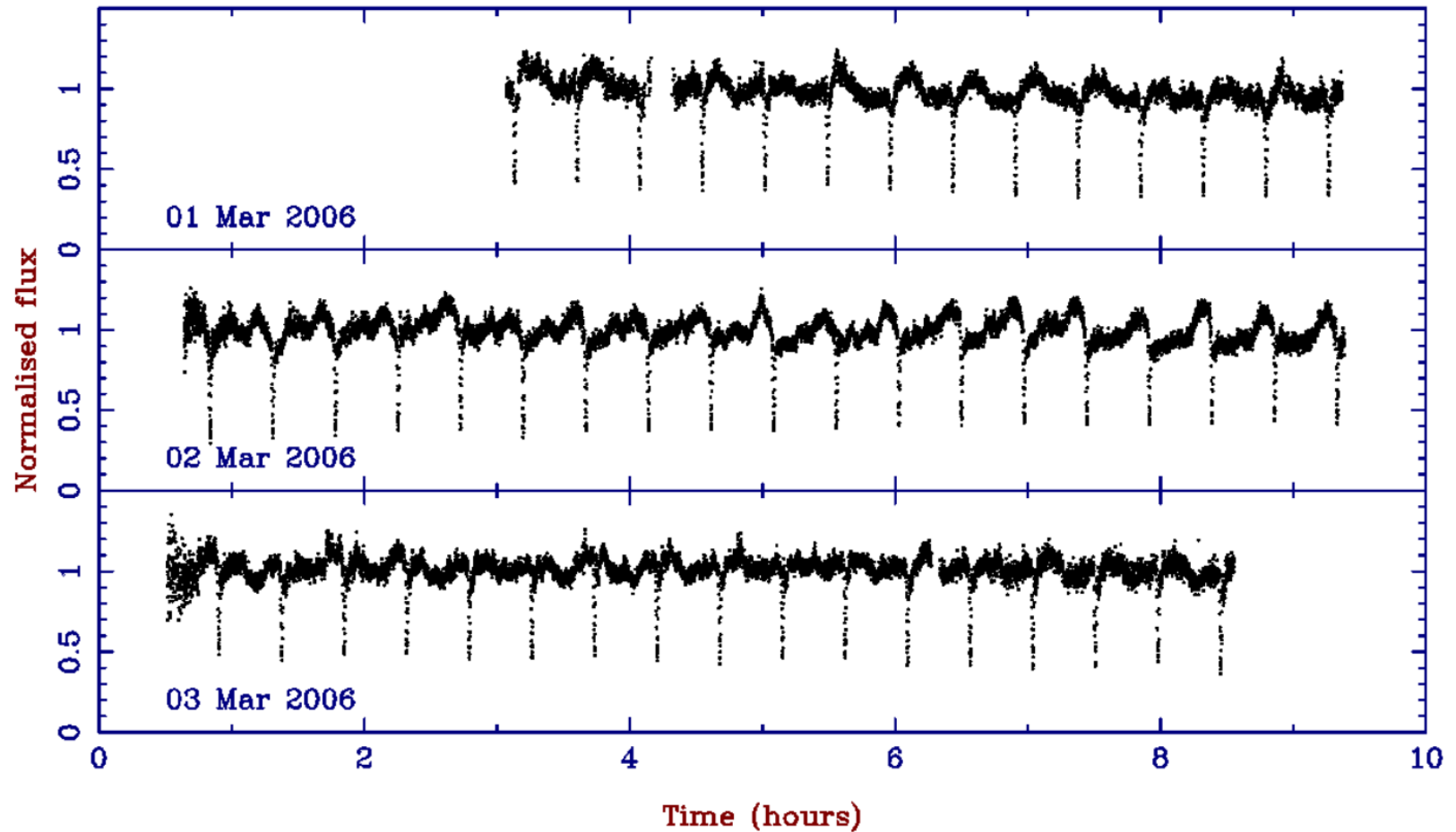
Our first chance to  
measure  
component masses  
directly.



Anderson et al (2005)

# SDSS0926+3624 with WHT+Ultracam

401

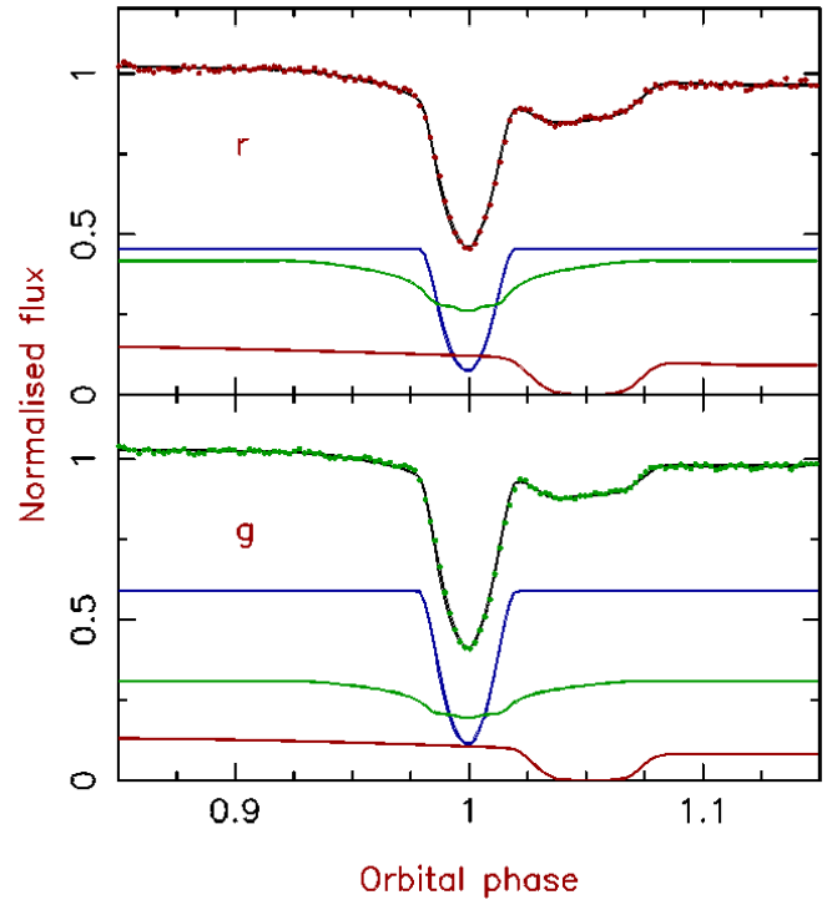


Interacting Binary Stars

# SDSS0926+3624 with WHT+Ultracam

402

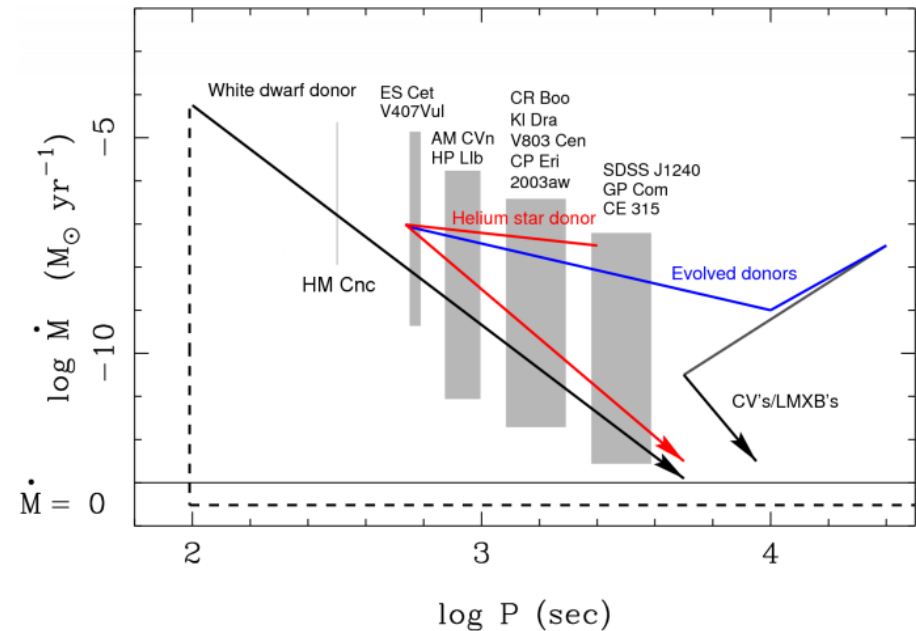
- Light curve fit  $\Rightarrow$   
 $M_2 = 0.029 \pm 0.002 M_{\odot}$ ,  
higher than expected for  
complete degeneracy  
( $0.019 M_{\odot}$ ).
- Indicates significant thermal  
energy in the donor,  
nevertheless it is consistent  
with a double white dwarf  
progenitor  
(Deloye et al 2007).



# AM CVn puzzles I. – their origin

403

- Three possibilities:
  - ▣ 1. Double white dwarfs (Paczynski 1967; Nelemans et al 2001).
  - ▣ 2. White dwarf/helium star binaries (Iben & Tutukov 1991).
  - ▣ 3. CVs with evolved donors (Posiadlowski et al 2003).
  
- Other than the possible-but-disputed 5 minute binary HM Cnc, all models can explain the orbital periods.



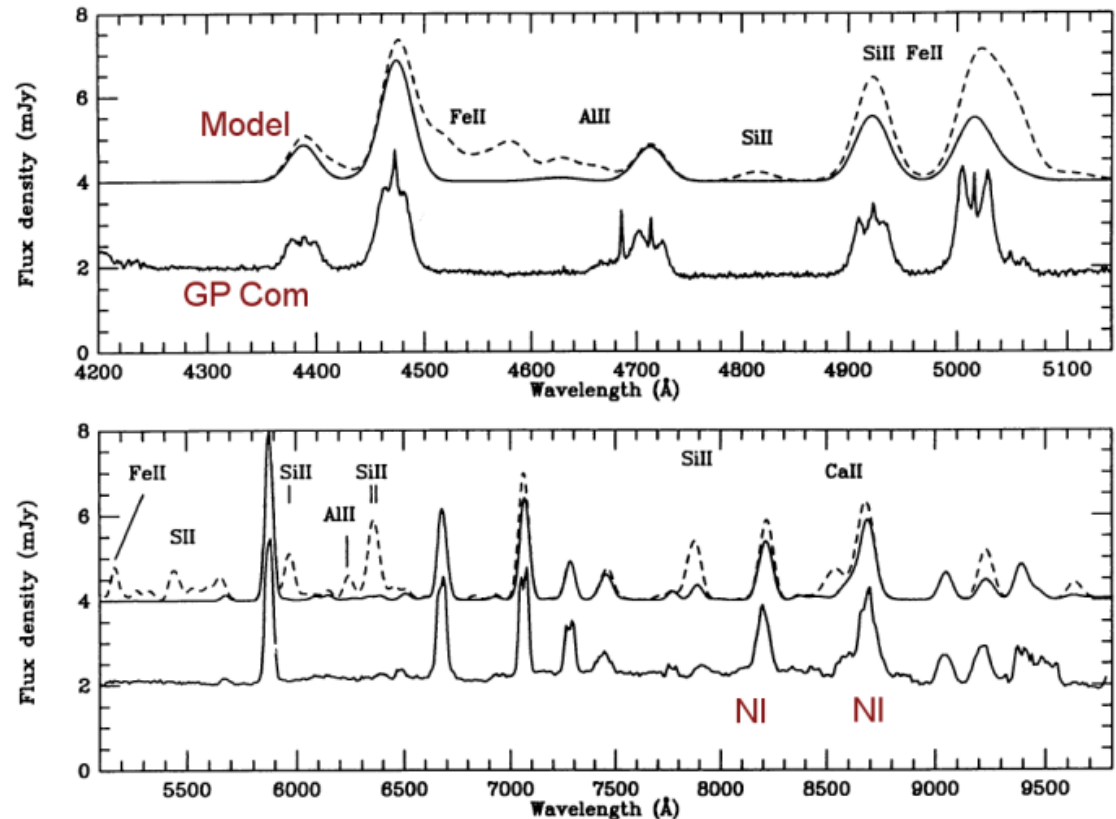
Nelemans et al (2001)

# AM CVn puzzles II. – abundances

404

**GP Com** appears to have  $\sim$  solar CNO/He (mostly N), but lacks Ca, Si and Fe.

However, the model (single-temperature LTE slab) is crude.

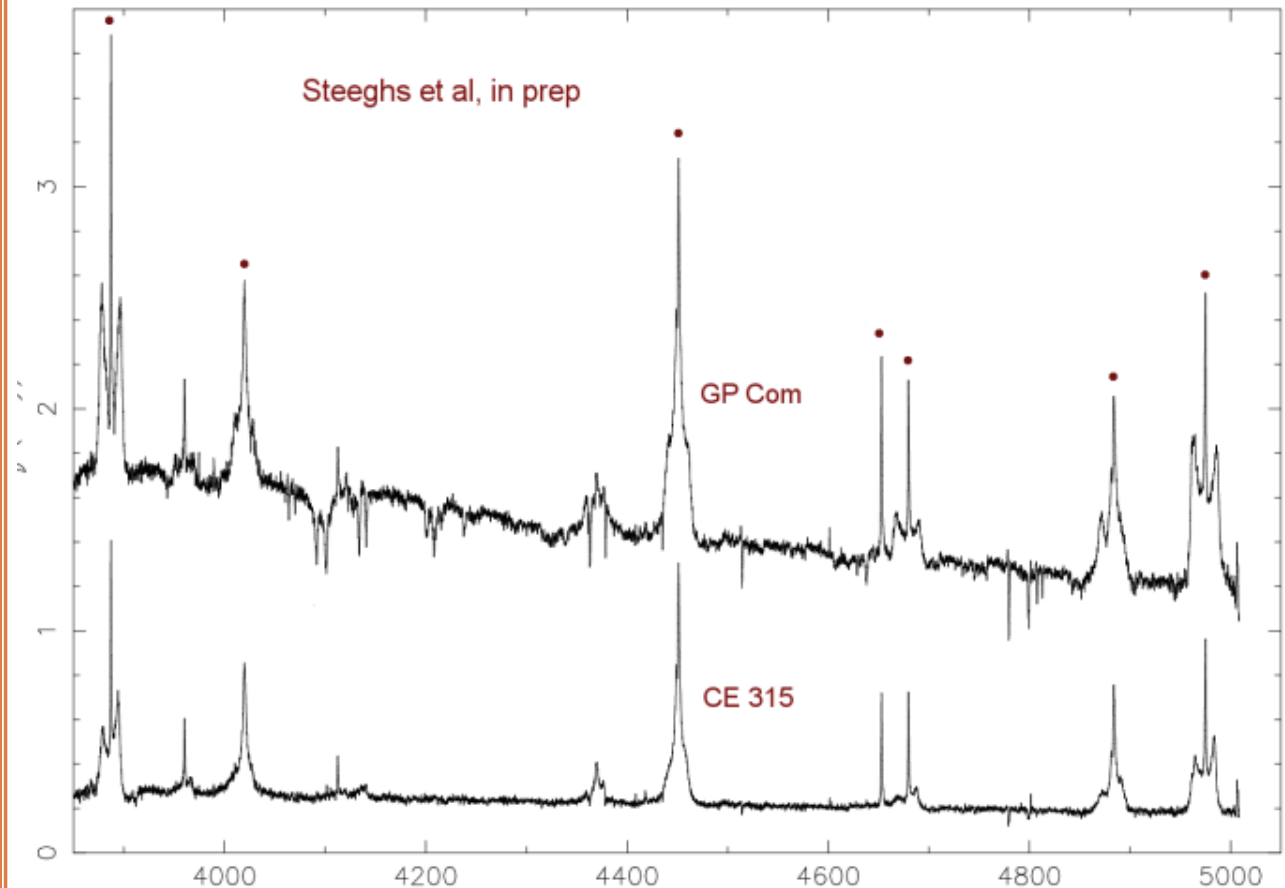


Marsh et al (1991)

# AM CVn puzzles III. – spikes

405

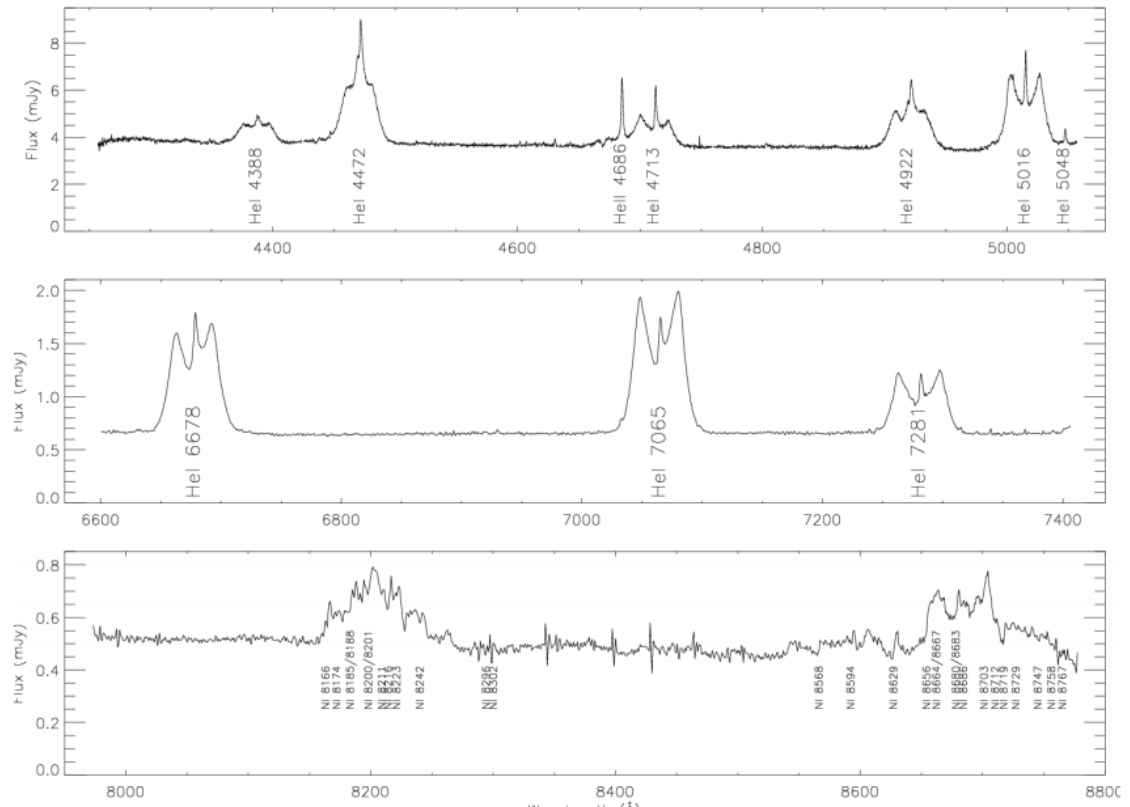
Several systems show sharp components at the centres of the double-peaked lines from the disks.



# AM CVn puzzles III. – spikes

406

Several systems show sharp components at the centres of the double-peaked lines from the disks.



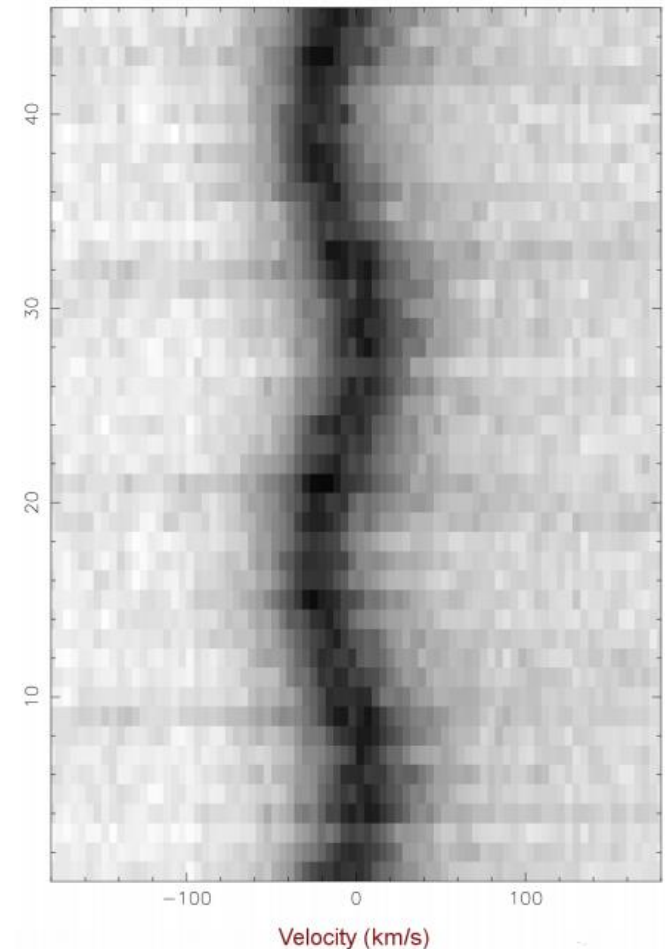
GP Com, Morales-Rueda et al (2003)



# AM CVn puzzles III. – spikes

407

- Kinematic constraints show that they come from the accreting white dwarfs, (Marsh 1999)  
⇒ slow rotation,  
 $v \sin i < 50 \text{ km/s}$ ,  
cf breakup  $\sim 5000 \text{ km/s}$ .

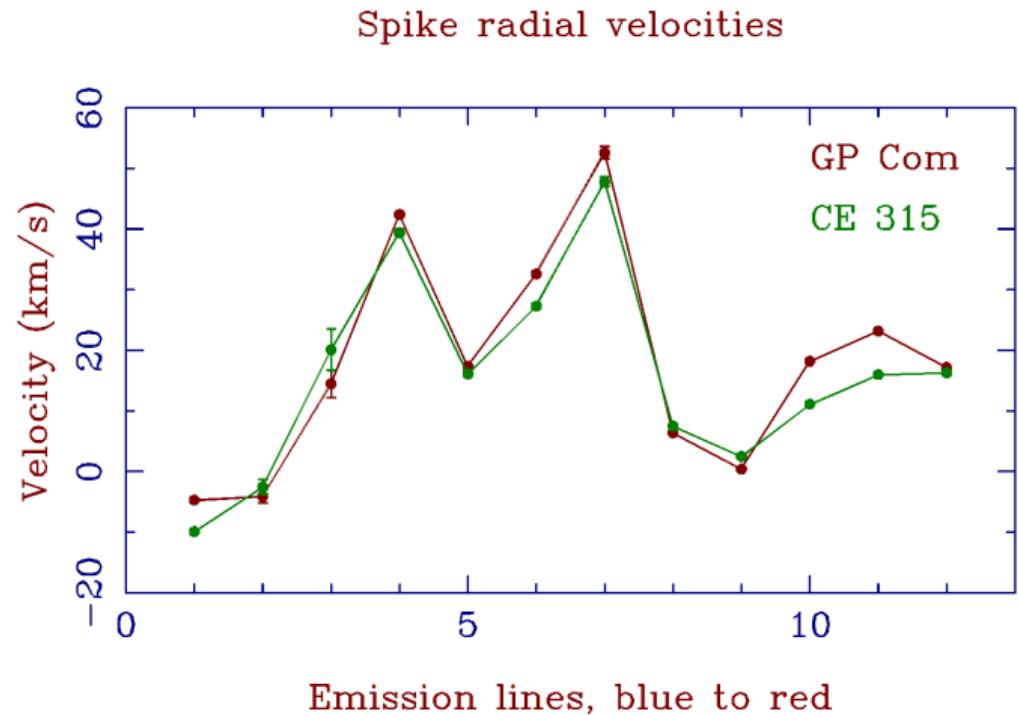


Interacting Binary Stars

# AM CVn puzzles III. – spikes

408

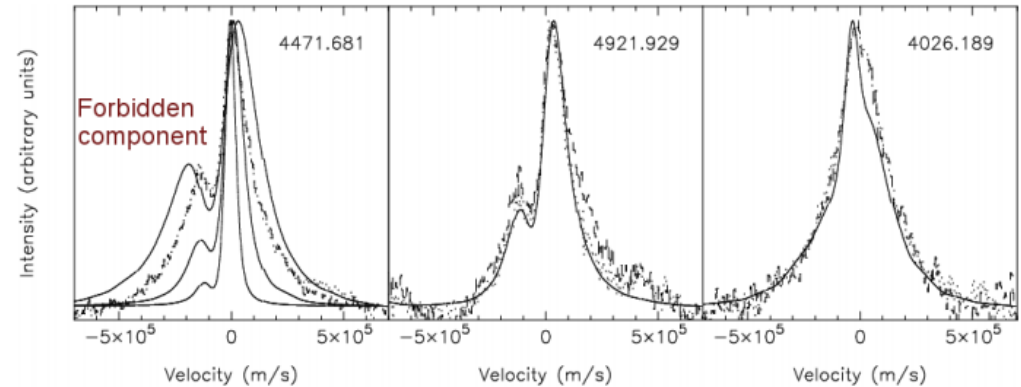
- Spikes should show a gravitational redshift, but the mean spike velocity is observed to vary from line-to-line.



# AM CVn puzzles III. – spikes

409

- Spike shifts & profiles probably the result of Stark broadening (Morales-Rueda et al 2003)
- $n_e \sim 10^{15} - 10^{16} \text{ cm}^{-3}$

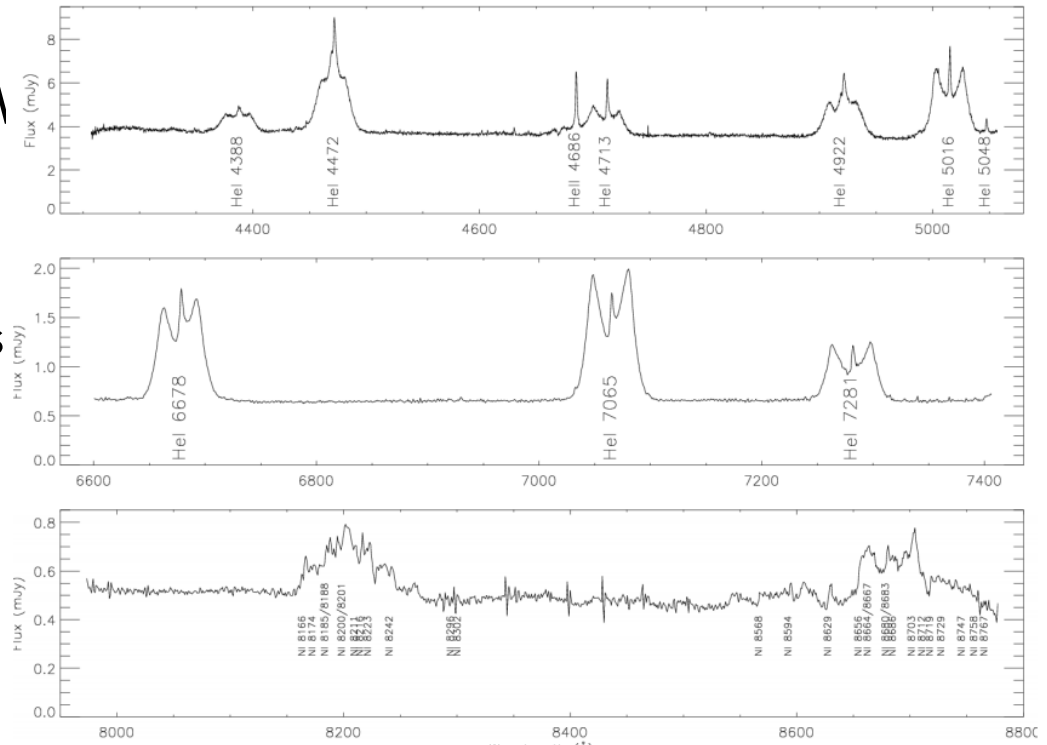


Steeghs, Roelofs et al, based on models of  
Beauchamp et al (1997)

# AM CVn puzzles III. – spikes

410

- How do the spikes form?
- Why are they seen in AM CVn stars but not in hydrogen-rich CVs?
- Why are they not always seen in AM CVn stars?
- How can the accretors rotate so slowly?

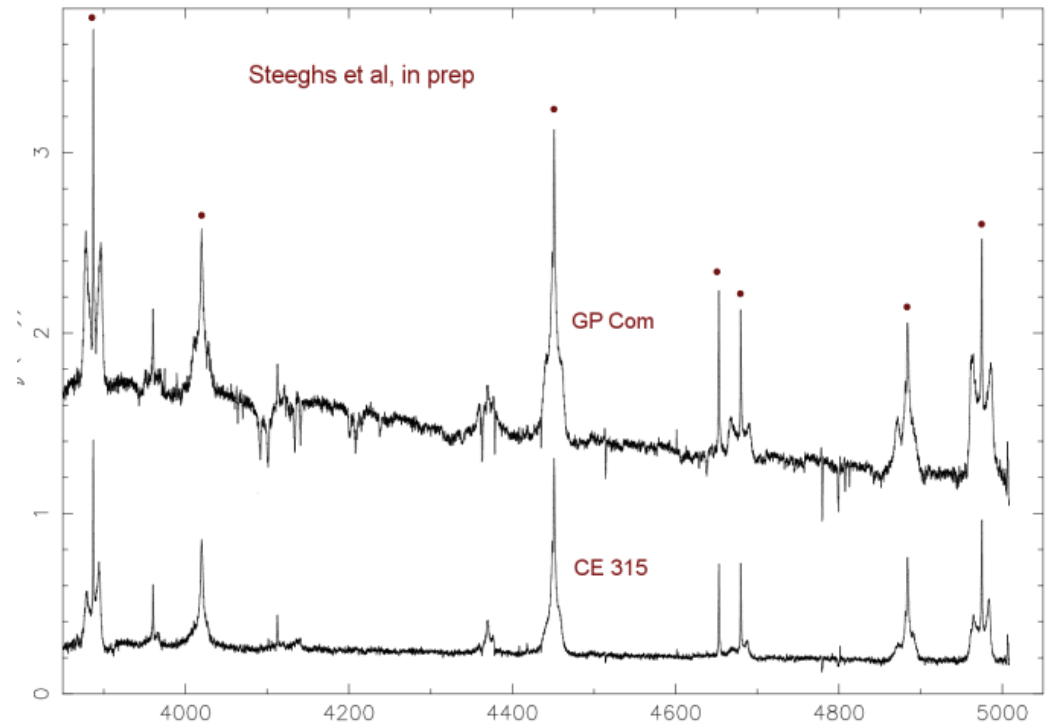


GP Com, Morales-Rueda et al (2003)

# AM CVn puzzles IV. – dips

411

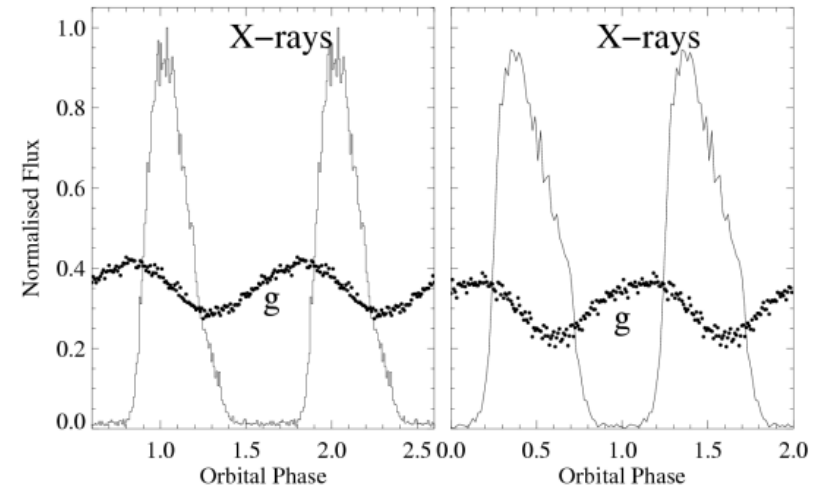
- Photosphere? If so, what element(s)?
- Time-variable? Accretion vs sedimentation. Critical  $\dot{M} \sim 10^{-12} M_{\odot} \text{ yr}^{-1}$  (Bildsten et al 2006).
- Request: cool white dwarf model atmospheres for 98% helium, 2% nitrogen plus heavier elements.



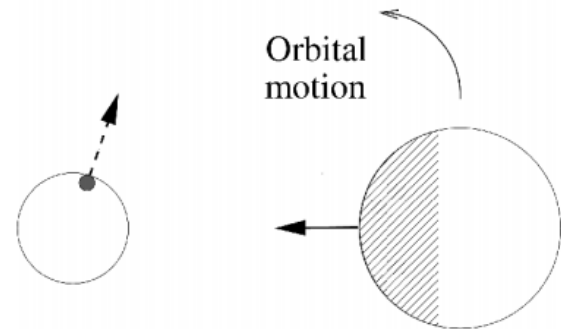
# The shortest period binaries?

412

- Two stars, V407 Vul and RX J0806+1527, have very similar light-curves and periods of 569 and 321 seconds.
- These are thought to be orbital periods  $\Rightarrow$  strong emitters of gravitational waves.
- If accreting, double white dwarf avoidance of mergers will be established.



Barros et al



Interacting Binary Stars

# AM CVn stars

413

1. The advent of large scale surveys has lead to the discovery of many new AM CVn stars.
2. The basic semi-detached, gravitational-wave driven model has held up well under the onslaught.
3. There have been significant advances in our understanding of the stellar components.
4. These stars pose a number of fascinating evolutionary and spectroscopic problems that we have yet to solve; the accretion disks remain an area of considerable uncertainty.
5. We need more good parameter estimates. These may only come from finding a few more of the million-odd systems in our Galaxy.

414

# X-ray Binaries

LMXBs

HMXBs



# X-ray Binaries

415

- X-ray binaries are a class of binary stars that are luminous in X-rays.
- They were among the first X-ray sources to be discovered (apart from the Sun and other Solar System sources).
  - ▣ Sco X-1 and Cyg X-1 were the first X-ray sources to be discovered in the constellations of Scorpius and Cygnus respectively and they are both X-ray binaries.

# Black Body Radiation (1)

416

- Light can be produced in many ways. The most fundamental source of radiation is a so-called “black body”.
- A black body is an idealized physical body that absorbs all incident electromagnetic radiation. Because of this perfect absorptivity at all wavelengths, a black body is also the best possible emitter of thermal radiation.
- Black body radiation is thus radiation which is in thermal equilibrium and which continuous spectrum depends only on the body's temperature.

# Black Body Radiation (2)

417

Depending on its temperature  $T$ , a black body emits radiation according to Planck's law:

$$L_{\lambda}(T) = \frac{2 h c_0^2}{\lambda^5} \left[ \exp \left( \frac{h c_0}{\lambda k_B T} \right) - 1 \right]^{-1}$$

where  $k_B = 1.38 \times 10^{-16}$  erg/K is the Boltzmann constant and  $L_{\lambda}(T)$  is the spectral radiance at the wavelength  $\lambda$ .

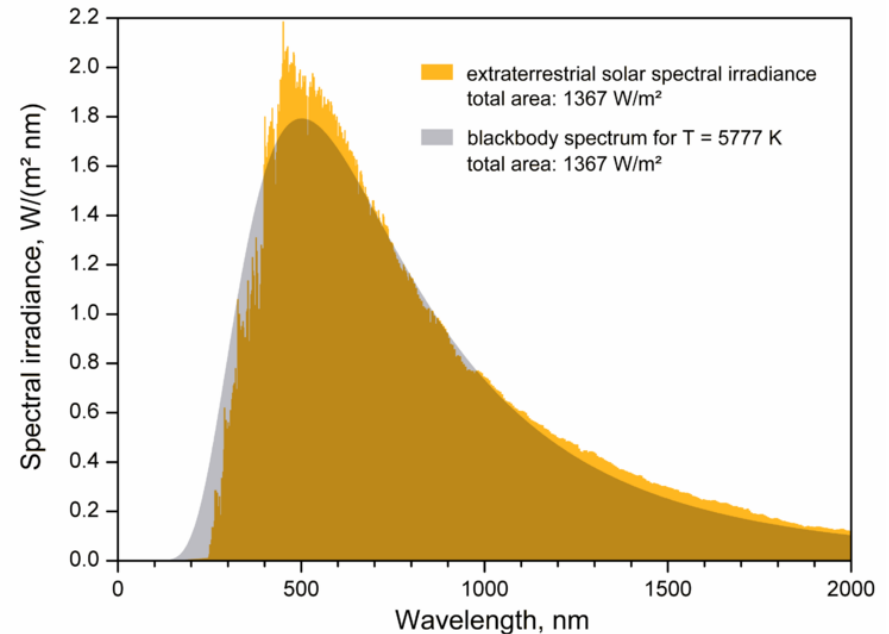
The corresponding formula for  $L_{\nu}(T)$  is

$$L_{\nu}(T) = \frac{2 h \nu^3}{c_0^2} \left[ \exp \left( \frac{h \nu}{k_B T} \right) - 1 \right]^{-1}$$

# Black Body Radiation (3)

418

- A black body is the extreme case of an optically thick medium. In the Universe, many plasma systems emit radiation approximately according to Planck's law, at least, in certain wavelength ranges.

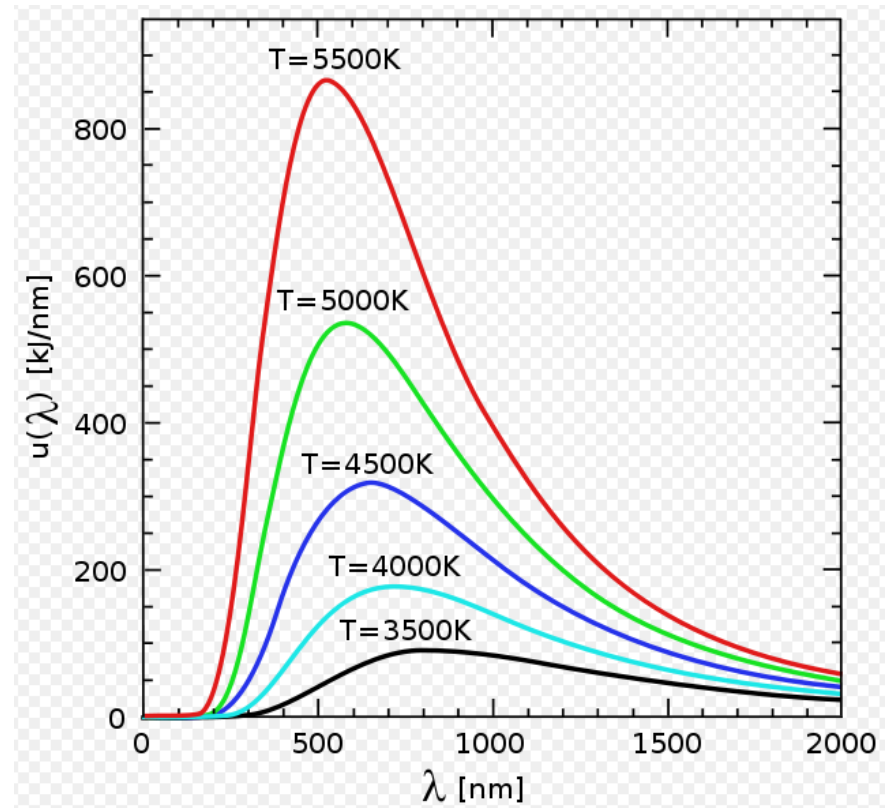


# Properties of the blackbody spectrum

419

- As the temperature increases, the peak of the blackbody radiation curve moves to higher intensities and shorter wavelengths.
- Wien's displacement law:  
 $\lambda_{\max} \approx 0.29(\text{cm})/T$   
 $\lambda_{\max}$  is a function only of the temperature

For  $T=10^7$  K we have  $\lambda_{\max} \approx 2.9 \text{ \AA}$   
This is a typical X-ray wavelength range



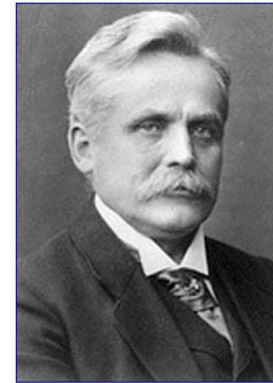
$L(T+\Delta T) > L(T)$  at all  $\lambda$  for positive  $\Delta T$

# X-ray Photons

420

## □ **Wien's Displacement Law (1893):**

$$T = 5 \times 10^7 \text{ }^\circ\text{K} / \lambda_{\text{max}} \text{ (Angstroms)}$$



→ 10 Angstroms  
is very hot !

Wilhelm Carl Werner Otto Fritz Franz Wien

## □ **X-rays: Photons 0.6-12 Angstroms → Energies 20-1 keV**

- Thermal Equivalent  $kT = 4 \text{ to } 80 \text{ million } ^\circ\text{K}$
- Heating mechanisms → non-thermal processes
  - synchrotron radiation (high energy  $e^-$  in  $B$  field)
  - inverse Compton (photon upscattered by high energy  $e^-$ )

# Energetics of accretion (1)

421

- The accretion of gas onto a compact object can be a very efficient way of converting gravitational potential energy into radiation.
- The amount of energy released by accreted gas is

$$E_{acc} = \frac{GM_*\dot{M}}{R_*}$$

$M_*$  and  $R_*$  are the mass and radius of the accreting star.

- By comparison, the conversion of the hydrogen into helium would yield an energy

$$E_{H \rightarrow He} \approx 0.007 \dot{M} c^2$$

# Energetics of accretion (2)

422

- Efficiency of the accretion process (fraction of the nuclear fusion [hydrogen to helium] energy that is radiated) is

$$\frac{E_{acc}}{E_{H \rightarrow He}} \approx \frac{GM_* \dot{M}}{0.007 \dot{M} R_* c^2} \approx \frac{70 R_{Sch}}{R_*}$$

$$R_{Sch} = \frac{2GM_*}{c^2} \approx 3km \frac{M_*}{M_\odot} \rightarrow \text{The Schwarzschild radius}$$

- Thus, accretion on to a compact object with  $R_* \leq 70 R_{Sch}$  is a more efficient mechanism than nuclear fusion of hydrogen to helium.



# Energetics of accretion (3)

423

- **A white dwarf:** typical mass  $2 \cdot 10^{30} \text{g}$  ( $1 M_{\odot}$ )  
 $R = 7000 \text{ km} \gg 70 R_{Sch}$
- **A neutron star:** typical mass  $3 \cdot 10^{33} \text{g}$  ( $1.5 M_{\odot}$ )  
 $R = 10 \text{ km} \ll 70 R_{Sch}$
- **A black hole**

**Accreting neutron stars and black holes are luminous sources, normally in X-ray radiation.**

Where does accreted matter come from? ISM?

No – captured mass is too small. Companion? Yes.

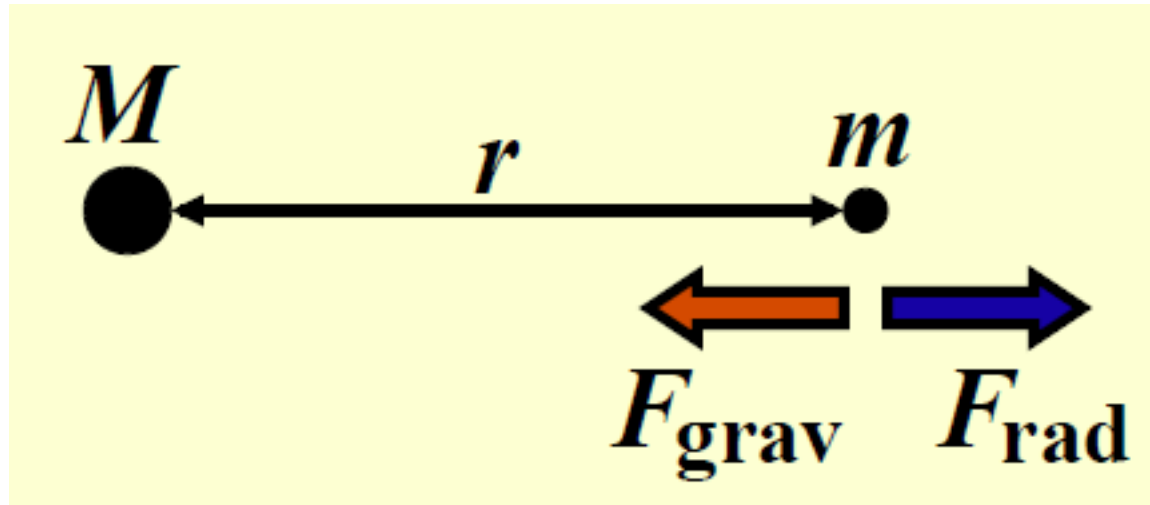
# The Eddington Luminosity (1)

424

- There is a (not strict) limit to the rate  $\dot{M}$  at which a compact object can accrete matter.
- Accordingly, there is a limit to the luminosity that can be produced by a steadily accreting object, known as the **Eddington luminosity**.
- Effectively it is reached when the inward gravitational force on matter is **balanced** by the outward transfer of momentum by radiation.

# The Eddington Limit (1)

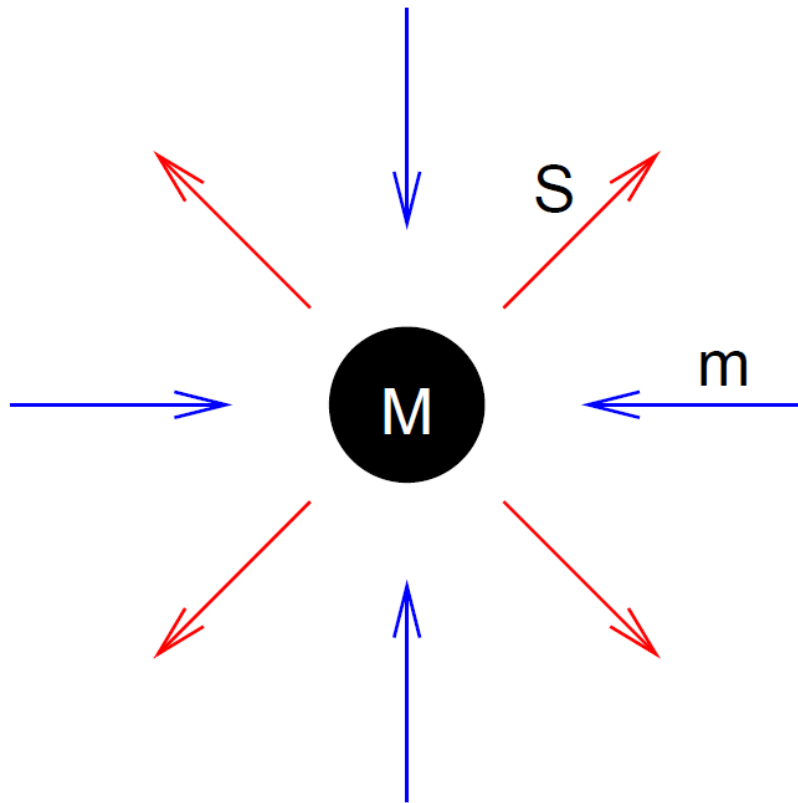
425



Accretion rate controlled by momentum transferred  
from radiation to mass

# The Eddington Limit (2)

426



- Assume mass  $M$  spherically symmetrically accreting **ionized hydrogen gas**.
  - Inward force: **gravitation**:
- $$F_{grav} = \frac{GM_* m_p}{r^2}$$
- At radius  $r$ , accretion produces **energy flux  $S$** :

$$S = \frac{L}{4\pi r^2}$$

- The luminosity  $L$  of the central compact object exerts a radiation force on the free electrons by **Thomson scattering**:

$$F_{rad} = \frac{\sigma_T S}{c}$$

- **Note:** the Thomson cross-section of protons is  $\sim 10^6$  times smaller than that of electrons. But: electrostatic forces between electrons and protons bind them so they act as a pair:  **$F_{rad}$  also has effect on protons!**

# The Eddington Limit (3)

427

- Accretion is only possible if gravitation dominates:

$$\frac{GM_* m_p}{r^2} > \frac{\sigma_T S}{c} = \frac{\sigma_T}{c} \frac{L}{4\pi r^2}$$

- and therefore

$$L < L_{Edd} = \frac{4\pi G M_* m_p c}{\sigma_T}$$

where  $L_{Edd}$  is called **the Eddington luminosity**.

- or, in astronomically meaningful units

$$L < 1.3 \times 10^{38} \text{ erg s}^{-1} \frac{M}{M_\odot}$$

- When the luminosity of the central compact object is greater than this value, the surrounding hydrogen gas will be blown away by the radiation pressure.

# The Eddington Luminosity (2)

428

- If the Eddington luminosity is emitted as black-body radiation, the temperature will be

$$T_{bb} = \left( \frac{L_{\text{Edd}}}{4\pi R_*^2 \sigma_{SB}} \right)^{1/4} = \left( \frac{GM_* m_p c}{R_*^2 \sigma_{SB}} \right)^{1/4}$$

where  $\sigma_{SB}$  is the Stefan-Boltzmann constant, and  $R_*$  is the radius of the surface from which the radiation is emitted (for a black hole, of course, this surface will be outside the Schwarzschild radius).

- For a black hole accreting at the Eddington limit, the temperature of the radiation will be  $T_{bb} \sim 4 \times 10^7 \text{ K } (M_*/M_\odot)^{-1/4}$ , if the radiation comes from immediately outside the Schwarzschild radius.
- The spectrum of the emitted photons will then peak at a photon energy  $E \sim 20 \text{ keV } (M_*/M_\odot)^{-1/4}$ .

# Maximum Accretion Rate

429

- The existence of the Eddington luminosity implies the existence of a maximum accretion rate,  $\dot{M}_{Edd}$ , for an accreting compact object. If the accretion energy  $E_{acc}$  is converted entirely into radiation, then the luminosity is  $L_{acc} = GM_*\dot{M}/R_*$ , and the maximum possible accretion rate is

$$\dot{M}_{Edd} = \frac{4\pi m_p c R_*}{\sigma_T} = 9 \times 10^{16} \text{ g sec}^{-1} \left( \frac{R_*}{1 \text{ km}} \right) = 1 \times 10^{-3} \text{ M}_{\odot} \text{ yr}^{-1} \left( \frac{R_*}{R_{\odot}} \right)$$

- In reality, the conversion is not 100% efficient, the accretion is not perfectly spherically symmetrical, and the radiation is not perfectly spherically symmetrical; thus, matter can be accreted at rates somewhat greater than  $\dot{M}_{Edd}$ .